

Development of Metrics for Resilience Quantification in Energy Systems

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ABSTRACT

The design of energy systems usually requires technical, economical and environmental analysis. However, the growth of systems failure due to unpredictable low-probability external events makes the consideration of resilience in this design also important. Although there is no standard metric for resilience quantification yet, it is known that it should consider system configuration, operation time and total or partial energy generation during and after the event, as well as the components repair probability and time. A proposal for resilience quantification in four cogeneration plants was previously developed based on components stochastic failures and verification of their consequences in the plant energy generation. The present work aims to continue the development of this metric by including in its calculation the repair probability of the components, their repairing time and the plant downtime during the repair, essential parameters for resilience quantification. Two new metrics are proposed and simulations with 0, 50% and 75% of repair probability of the components are made in software *CLIPS*. One of the metrics is able to evaluate the influence of repairment in system resilience, while the other one predicts plant downtime during operation. The metrics point to S#2 as the most resilient system and S#3 as the most affect by repairing.

1. INTRODUCTION

The development of actual society is fully dependent on energy, which has its demand continuously increased over time. Energy systems have been studied technically and structurally, in order to enhance power supply and increase both efficiency and reliability.

Regarding technical aspects, the design of energy systems usually considers energy balance, as well as economical and

environmental analysis. In this context, power plants working with cogeneration technology stand out due to their high conversion efficiency and capacity to generate power and useful thermal energy (cooling or heating) simultaneously from a single fuel source (Silva, Matelli and Bazzo, 2014). Additionally, these systems have flexibility to operate in several places such as industries, residential buildings and hospitals (Isa, Tan and Yatim, 2018). Although many equipment can be used as prime movers, internal combustion engines and gas turbines are currently the most attractive, since they have commercial advantages when compared to other components (Matelli & Goebel, 2018).

Structural analyses of energy systems depend mainly on reliability concepts, which consider expected events to predict failure of components and, consequently, of the whole plant. However, the growth of failures due to unpredictable low-probability high-impact external events in the last years increased the structural vulnerability of these systems (Shen, Gut and Zhao, 2019). To evaluate the consequences of such events, a recent approach focused on resilience has been introduced.

Resilience can be defined as the ability of the system to operate totally or partially at some functional level under scenarios before, during and after low-probability high-impact events. It also includes its capacity to withstand and recover quickly from unexpected disruptions (Sandia National Laboratories, 2014).

According to Hickford, Blainey, Hortelano and Pant (2018) and Francis and Bekera (2014), a resilient system must be able to absorb, adapt and recover from unpredictable situations. The absorptivity is related with the impact that the system can withstand before its partial or total disruption, as long as the recovery capacity is related to how rapidly the system can return to its partial or total functional operation after the event. The adaptation is the ability of the system to change some features in its structure in response to an adverse situation caused by an event, in order to continue its operation at some functional level.

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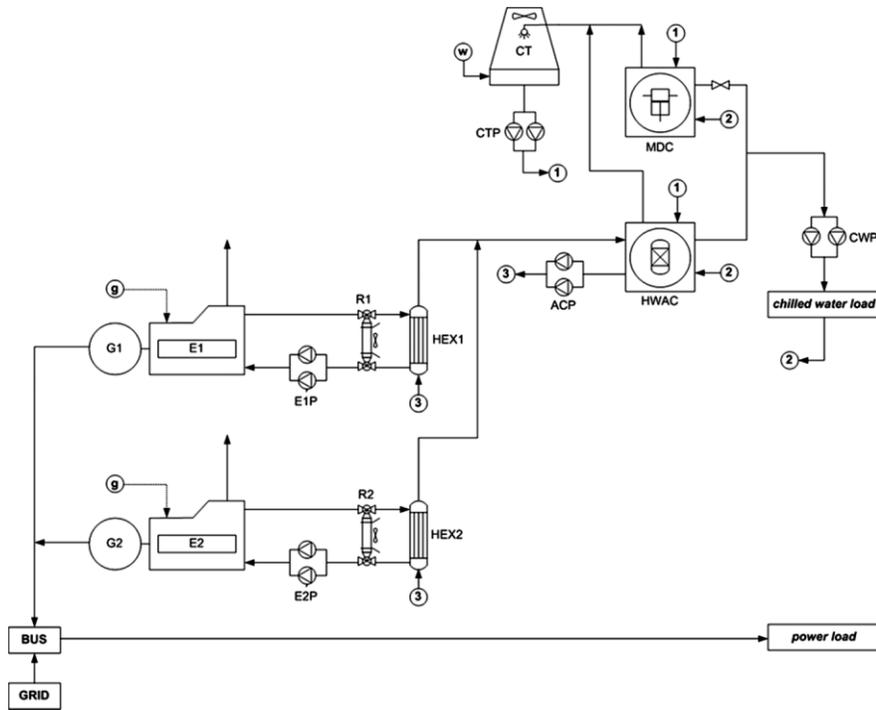


Figure 2. S#2: system based on two internal combustion engine generation

As it can be seen, the capital difference between S#1 and S#2 is the number of internal combustion engines (E) coupled to the respective generator (G), which is connected to a bus bar along with the external grid, meeting the previously requested power load. A heat exchanger (HEX) is used to produce hot water from the heat associated to the engine jacket water. The produced hot water feeds a single effect absorption chiller (HWAC), in order to produce enough chilled water as

demanded. A radiator (R) is connected to the engine to keep it operating when the HWAC is off. A mechanical-driven chiller (MDC) can suit as supplement or backup. Lastly, a cooling tower (CT) rejects the heat released from both chillers.

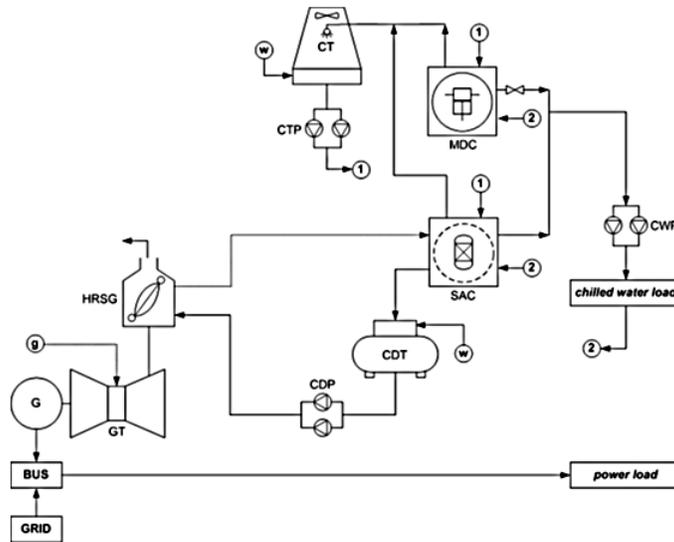


Figure 3. S#3: system based on one gas turbine generation

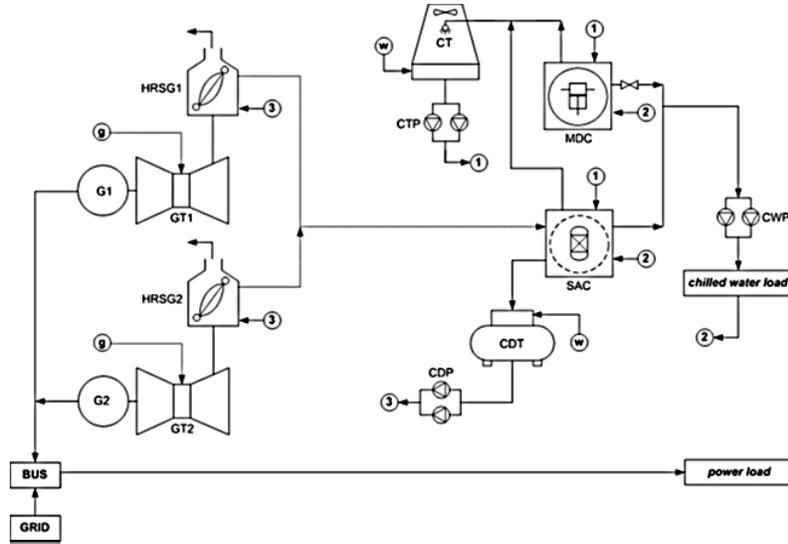


Figure 4. S#4: system based on two gas turbines generation

As in the internal combustion engine-based systems, S#3 and S#4 also differ by the number of prime movers, in these cases a gas turbine (GT). GT is coupled to a generator (G), which feeds the bus bar along with the external grid, in order to meet the specified power load. GT exhaust gases reject heat in a heat recovery steam generator (HRSG), where steam is produced to feed a double effect absorption chiller (SAC), in order to meet the requested chilled water demand. A mechanical-driven chiller (MDC) can suit as backup. Finally, a cooling tower (CT) rejects the heat released from both chillers.

Information about systems thermal performances can be found in Silva et al. (2014).

2.2. Simulation framework

The four cogeneration plants are modeled in software ‘C’ *Language Integrated Production System* (CLIPS), specifically designed to develop knowledge-based systems. Simulations of stochastic failure of components are performed with Monte Carlo approach, i.e., with several repetitions at the same conditions in order to verify standard operation responses for each configuration.

The simulations proceed as follows: a non-failed component *i* is randomly chosen as a candidate to fail. A failure probability (p_b) is randomly assigned and compared to a known probability of component normal operation (p_i). If $p_b > p_i$, the component *i* fails, otherwise a new choice is made. In case of failure, all the components connected to the component *i* and to the propagated failed components are checked, in order to verify the failure propagation throughout the system. Failure propagation rule is illustrated in Figure 5.

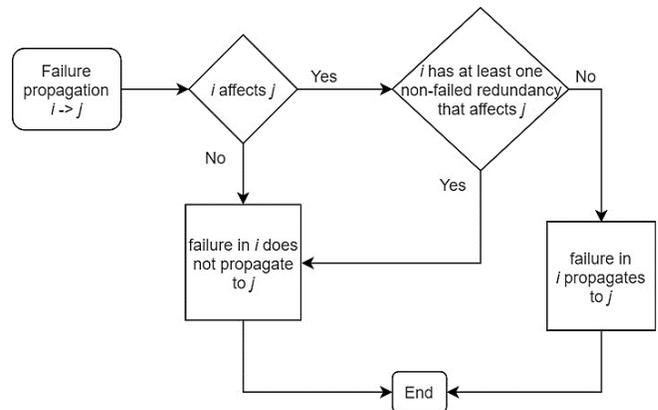


Figure 5. Failure propagation rule

Once the failure propagation is verified, a repair probability (p_{cr}) is randomly assigned and compared to a known non-viability repair probability (p_{cnr}). If $p_{cr} > p_{cnr}$, component *i* starts the repair process, otherwise it keeps failed until the end of the simulation. In repairing processes, the time spent in repair (ts) increases in a unity every hour of plant operation until it reaches the repair time (rt). Then, the component *i* and all the components that failed by propagation return to their non-failed condition.

Considering all scenarios of failure throughout the simulation, the functional state of the system can be classified in three ways:

- Normal: the system has no failed components and, therefore, meet power and chilled water demand completely;

The simulation requires two parameters to start: system expected operation time, T , and number of simulations, N .

The proposed modeling considers the following assumptions:

- $T = 8760$ h, simulating a whole year of uninterrupted operation, and N is fixed in 3000 simulations, enough to stabilize the coefficient of variation (Matelli & Goebel, 2018);
- All the components have constants and time-independent p_i and p_{cnr} ;
- Each component repairing time follows the values assumed in Table 2;
- Failure propagation considers all the components connected to original failed one, regardless of the nature of the connection, with constant and time-independent propagation probability equal to 1;
- Component functional state is either failed or normal, with no partial operation admitted.

The value of p_i is assumed to be 0.9995 as in Matelli and Goebel (2018), focusing on results comparison, as long as it was assigned three different values to p_{cnr} : 1, 0.50 and 0.25. The first value is assigned to keep the simulation with no repair probability, in order to compare the results with the previously work; the second one intends to keep the component repairing at chance (i.e., the repairing success is no better than a flip coin); the third value leads to greater repair probability, which provides clearer information about the influence of the repairing success in the system resilience. Repair times shown in Table 2 were assumed considering components function in order to standardize proportional values.

Table 2. Components repairing time

Function	Repairing time (h)	Component
Shaft work generation	100	Turbine
		Engine
Power generation	80	Generator
Heat exchange	60	Hot water absorption chiller
		Mechanical chiller
		Heat exchanger
		Steam absorption chiller
		Heat recovery steam generator
Feeding	40	Cooling tower
		Radiator
		Chilled water pump
		Hot water chiller pump
		Jacket water pump
Structural	40	Cooling tower pump
		Condensate pump
		Grid
		Bus
		Power load
Storage	30	Chilled water load
		Gas line
		Water line
		Condensate tank

2.3. Metrics for resilience quantification

Considering the simulation framework previously described, two new metrics (vi and vii) are proposed in this work to complement the five metrics (i-v) developed by Matelli and Goebel (2018).

- Fraction of simulations with resilient operation (p_r): ratio between the number of simulations k in which $t_k = T$ and $0 < r < t_k (N_r)$ and the total number of simulations N . It can be interpreted as the probability of the system to operate at resilient functional state. The higher p_r , the higher the system resilience.

$$p_r = \lim_{N \rightarrow \infty} \left(\frac{N_r}{N} \right) \quad (1)$$

- Resilient operating time (\bar{r}): weighted average of the resilient operating time r for all N_r simulations, in which $t_k = T$ and $0 < r < t_k$. It indicates which system can operate in a resilient condition for longer periods.

$$\bar{r} = \frac{p_r}{N_r} \sum_{k=1}^{N_r} r_k \quad (2)$$

- Time until failure (\bar{f}): average time for all simulations k in which $t_k < T$ and $r_k < t_k$, i.e., all simulations that result in a total system failure before admitted lifetime (N_f). Higher value of this parameter indicate system with enhanced resilience.

$$\bar{f} = \frac{1}{N_f} \sum_{k=1}^{N_f} t_k \quad (3)$$

- Fraction of simulations with completely failed operation (p_f): relation between the number of simulations k in which $t_k < T$ and $r_k < t_k (N_f)$ and the total number of simulations N . It can be interpreted as the probability of the system to fail. Systems with lower resilience exhibit high p_f .

$$p_f = \lim_{N \rightarrow \infty} \left(\frac{N_f}{N} \right) \quad (4)$$

- Normalized resilience index (ρ): an average operating time (\bar{t}) is firstly calculated considering the system failure probability (p_f) and its complementary value, as expressed in Eq. 5. Therefore, the parameter \bar{t} is a weighted average between the time in simulations in which the system fails completely and the time in simulations that result in operation until its admitted lifetime. Then, \bar{t} is normalized regarding T (Eq. 6).

$$\bar{t} = p_f \bar{f} + (1 - p_f) T \quad (5)$$

$$\rho = \frac{\bar{t}}{T} \quad (6)$$

The closer ρ is to the unity, the higher the system resilience.

- vi. Fraction of simulation with system recovery (p_d): ratio between the number of simulations k in which $t_k = T$ and $d_k > 0$ (N_d) and the total number of simulations N .

$$p_d = \lim_{N \rightarrow \infty} \left(\frac{N_d}{N} \right) \quad (7)$$

A higher number of k simulations that result in system failure with recuperation (N_d) indicates a higher number of failures during the operation, but with high rate of successful repairs. In the limit case where all repairing actions are unsuccessful, the value of p_d gets closer to p_f when no repairing actions are taken, i.e., $p_d \approx p_f$. Therefore, the higher the difference $p_f - p_d$, the higher the impact of repairing actions on the system resilience.

- vii. System downtime (\bar{D}): weighted average of the plant downtime d for all k simulations with $t_k = T$ and $d_k > 0$ that result in system failure with recovery (N_d). It indicates how long the system remains failed before return to normal operation. Therefore, the lower this parameter, the higher system resilience.

$$\bar{D} = \frac{p_d}{N_d} \sum_{k=1}^{N_d} d_k \quad (8)$$

3. RESULTS AND DISCUSSION

Although thermal performance and system costs are not discussed herein, Silva et al. (2014) found that from that perspective, the preferred system choice would be S#1, followed by S#2, S#3 and S#4, respectively. Regarding initially proposed resilience metrics, the numerical results that Matelli and Goebel (2018) (represented in Table 3 as M&G) found in their work with simulations considering no repairing actions are compared with the results of this work considering $p_{cnr} = 1$, i.e., also with no repairment. The comparisons are represented in Table 3.

Table 3. Comparisons of results from Matelli and Goebel (2018) with this work with no repairing.

Parameter/System	S#1	S#2	S#3	S#4
p_r (M&G)	0.516	0.654	0.456	0.568
p_r	0.490	0.638	0.453	0.581
\bar{r} (M&G)	3188	4245	2890	3619

\bar{r}	3013	4097	2722	3635
\bar{f} (M&G)	5057	5198	4849	5116
\bar{f}	5038	5317	4908	5049
p_f (M&G)	0.461	0.328	0.526	0.414
p_f	0.482	0.338	0.525	0.396
ρ (M&G)	0.805	0.867	0.765	0.828
ρ	0.795	0.867	0.769	0.832

As it can be noted in Table 3, all the metrics in both works point to system S#2 as the most resilient, followed by S#4, S#1 and S#3, respectively. With no repairing actions, it is clear that redundancy is the most impactful factor in resilience value.

The results of the seven metrics proposed in this work with $p_{cnr} = 0.25, 0.5$ and 1 are shown in Figures 7-13. Compared to results represented in Table 3, values presented in these figures indicate that repairing actions increase system resilience, as expected.

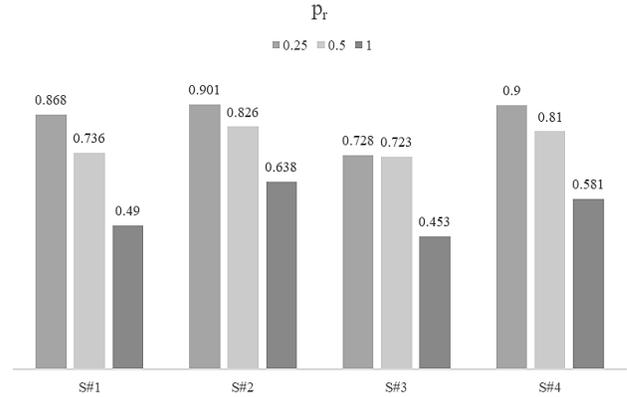


Fig 7. Variation of p_r with different p_{cnr} values

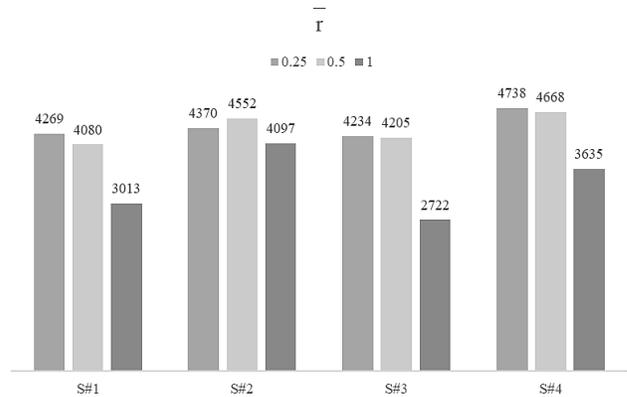


Fig 8. Variation of \bar{r} with different p_{cnr} values

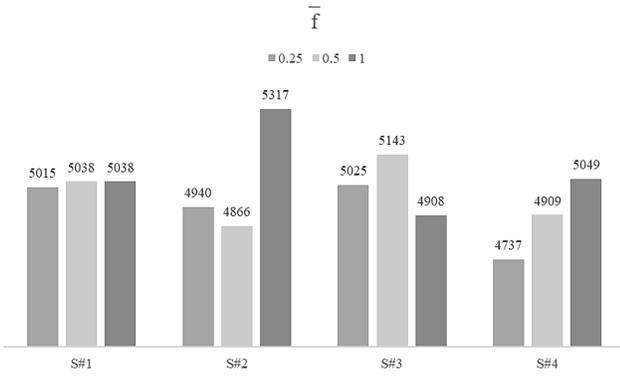


Fig 9. Variation of \bar{f} with different p_{cnr} values

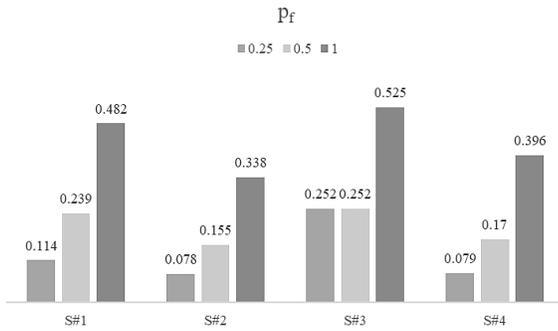


Fig 10. Variation of p_f with different p_{cnr} values

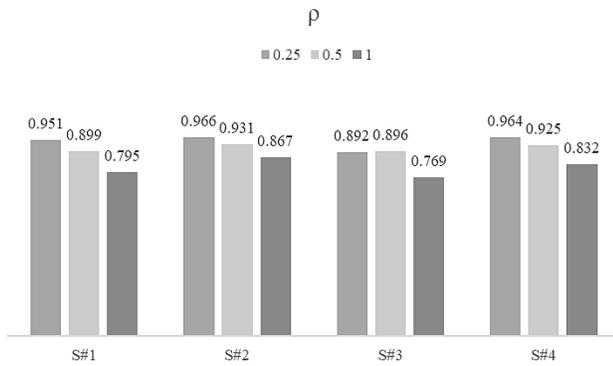


Fig 11. Variation of ρ with different p_{cnr} values

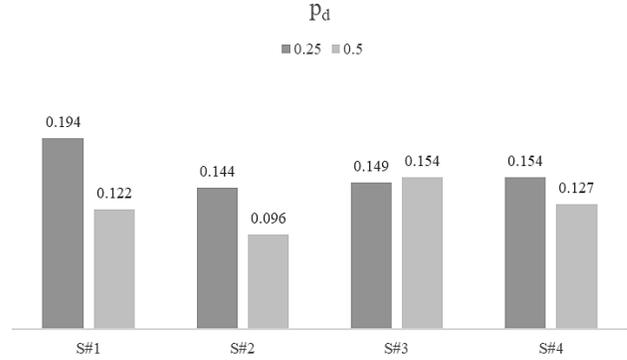


Fig 12. Variation of p_d with different p_{cnr} values

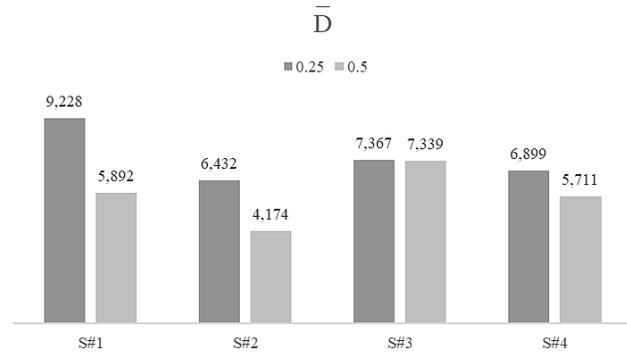


Fig 13. Variation of \bar{D} with different p_{cnr} values

All the configurations enhanced their probability of resilient operation, resilient operation time and resilience index with the addition of repair actions. It can be noted a decrease in probability of failure as well. It can also be observed a smaller difference between the maximum and minimum values of each parameter for all the proposed configurations. Resilient operating time, for example, exhibited variation of 46.9% and 50.5% for results in previously work and this work, respectively, as shown in Table 3, while the variation of the same parameter in Figure 8 is 5.7%. It indicates that in addition to enhance the resilience of all configurations, repairing actions also improved proportionally more the systems with lower resilience, i.e., with no redundancies. It becomes clearer when metric v_i is applied. The values of $p_f - p_d$ are, in ascending order for $p_{cnr} = 0.5$: 0.242 for S#2, 0.270 for S#4, 0.359 for S#1 and 0.371 for S#3. It can be observed that the S#3 is the most affected system when repairing actions are taken, while S#2 is the least one.

As the systems with redundancies presented greater resilience when repairing actions are disregarded, the improvement of resilience results in more simulations reaching $t_k = T$, i.e., until system lifetime. On the other hand, systems with no redundancies are expected to enhance their

time until failure, although they do not reach their lifetime so often, once the lack of redundancy is a factor that has high influence in system performance. This can explain the fact that S#2 and S#4 had their time until failure hardly decreased, while S#1 almost suffered no oscillation and S#3 increased its value.

With the increase of repair probability, there was an increase in the number of simulations with resilient operation, since component repairing success is more likely. It is also observed the improvement of resilience index and system downtime, although the last parameter do not present significant changes in S#3, which point to a system with no apparent resilience improvement. As the system with lowest resilience, S#3 seemed to reach its maximum with repair actions.

Regarding resilient operating time, systems S#1, S#3 and S#4 have this parameter increased. However, S#2 decreased its value with increasing repair probability, which can indicate a more normal time operation. This conclusion is also confirmed by the time until failure, which has increased, pointing to a system with more operating time. As S#2 is the most resilient one, it is expected that instead of enhancing its resilient operation time, the higher repair probability tends to increase its normal operation time.

Different from the results of simulations without repair, there is no convergence on which system is the most resilient according to data exhibited in Figures 7-13. With $p_{cnr} = 0.5$, metrics i, iv, v and vii point to the same sequence from the most to the least resilient system as found by Matelli and Goebel (2018): S#2 -> S#4 -> S#1 -> S#3. Metric ii confirms that the systems with redundancies have greater resilience values, although it was affected by the higher proportional improvement of systems with lower resilience when no repairing actions are taken.

However, iii diverges from the other metrics as it points to S#3 and S#1 as the most resilient ones, followed by S#4 and S#2, respectively. As discussed before, this can be caused by the increase of the number of simulations of systems with redundancies that reached lifetime.

When $p_{cnr} = 0.25$, metrics i, iv and v continued to point sequence S#2 -> S#4 -> S#1 -> S#3. Metric ii exhibited S#4 as the most resilient, once S#2 decreased its resilient operation time, as previously discussed. Metric iii indicated S#3 as the one with highest resilience. The new metric vii pointed to S#2 as the most resilient and S#1 as the least resilient. The difference $p_f - p_d$ proposed by metric vi showed smaller values compared to when $p_{cnr} = 0.5$, although S#3 seemed to be stabilized. This fact points to a high initial impact in resilience when repairing actions are taken, followed by a reduced impact when repair probability is enhanced. This difference showed that S#3 is the most affected system by repairing actions, followed by S#1, S#4 and S#2, respectively.

4. CONCLUSIONS

Four cogeneration systems were developed via *CLIPS* and seven metrics for resilience quantification were proposed herein, with two of them considering components repairing time, a new analysis in this methodology.

With no repairment, the first five metrics pointed to the same sequence of the most to the least resilient system. Four of the seven metrics in first simulation with repair pointed to S#2 as the most resilient system and S#3 as the least resilient one. In last simulation condition, with higher repair probability, there were also four metrics considering S#2 with higher resilience value and four of them pointing S#3 with the lowest.

It became clear the importance of repairing in resilience of these systems. With repair actions, all the systems enhanced their resilience, being the higher proportional increases in those with lower resilience. In systems with no redundancy, repairment hardly improved all the values of the metrics, indicating to be a good alternative for resilience actions. This fact could be reiterated with application of metric vi, which pointed to S#3 and S#1 as those who suffered more impact in their resilience with the addition of repairment.

Although S#1 exhibited higher thermal efficiency, S#2 presented higher resilience in almost all metrics, therefore being the most resilient one. Any project that considers resilience as an important factor must focus on redundancy and repair actions, as it can be concluded by this work.

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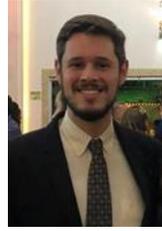
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Biographies



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