Integrating Model-Based and Data-Driven Simulator for Health Management of a Reusable Rocket Engine

Daiwa Satoh¹, Noriyasu Omata¹, Miki Hirabayashi¹, Seiji Tsutsumi¹, Kaname Kawatsu², and Masaharu Abe³

¹ Research Unit III, Research and Development Directorate, Japan Aerospace Exploration Agency (JAXA), Sagamihara, Kanagawa, 252-5210, Japan

> satoh.daiwa@jaxa.jp omata.noriyasu@jaxa.jp m_hirabayashi@office.so-net.ne.jp tsutsumi.seiji@jaxa.jp

² Research Unit III, Research and Development Directorate, Japan Aerospace Exploration Agency (JAXA), Tsukuba, Ibaraki, 305-8505, Japan kawatsu.kaname@jaxa.jp

³ Aerospace Engineering Solution Division, Business Headquarters, Ryoyu Systems Co., Ltd., Nagoya, Aichi, 455-0024, Japan abe.masaharu@jaxa.jp

ABSTRACT

There is considerable need to generate large amounts of training data that include various operating conditions for fault detection and diagnosis with machine learning in a reusable rocket engine. A system-level simulation model has been developed in which reduced-order models are employed to simulate the global behavior of a reusable rocket engine. Although some components of the engine are not modeled at the system level due to their complexity, they are included among the items inspected during fault detection and diagnosis. This study has developed a regression model for simulating the behavior of such components based on the results of static-firing tests on a reusable rocket engine developed in Japan. The regression model used measurements that can be modeled by the system-level simulation and treated the ones that cannot be modeled as response variables. To identify the operating conditions, the explanatory variables are divided using the Gaussian mixture model in advance, and the Ridge regression models are then trained from the clustered explanatory variables on each cluster. This method reasonably predicts the response variables, even if the static-firing testing includes varying operating conditions such as the combustion phase with varied throttling and the chill-down phase.

1. INTRODUCTION

Many countries have developed reusable launch vehicles to cut launch costs. Although reusable launch vehicles need regular maintenance to maintain reliability, maintenance accounts for most of the launch cost. Four approaches can improve maintenance cost-cutting: a design methodology with long service life as a major consideration; a technique for evaluating remaining component lifetime; nondestructive inspection technology; and fault detection and diagnostics. The authors focus on fault detection and diagnosis in this paper. Reusable launch vehicles need more launches to be operated more effectively. However, since rocket engines are complex and many sensors are needed to monitor the condition of the entire system, manual inspection is time consuming. Further, fault detection and diagnosis of a rocket engine must be finished quickly, so quick and reliable maintenance using only manual inspection has become no longer possible.

To solve the issue, the Japan Aerospace Exploration Agency (JAXA) has developed techniques for fault detection and diagnosis (Kawatsu, 2019; Tsutsumi et al., 2019) for the Reusable Sounding Rocket (RSR), which was developed in Japan (Nonaka et al., 2011; Sato et al., 2014; Kimura et al., 2016). The techniques require vast amounts of training data. Moreover, it is difficult to the anticipate launch conditions because of changing weather and flight conditions. Static-firing tests take a lot of time and are expensive, so preparing training data using only static-firing tests is also unrealistic.

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The authors have developed a System-Level Simulation (SLS) model to generate training data instead of relying on static-firing tests (Sato et al., 2019). The SLS model simulates the global behavior of an RSR engine by employing reduced-order models. The simulation results in steady-state are highly accurate and obtained by parameter estimation with data assimilation. By changing valve sequences and the pressure and temperature of the tanks, the SLS model can generate time series data under a variety of operating conditions. Many model-based approaches for various products in diverse fields have already been studied (Belapurkar et al., 2011; Frank et al., 2016; Zolghadri et al., 2016; Poon et al., 2017; Sobie et al., 2018; Chowdhury et al., 2019). These studies modeled their targets numerically and used their models for fault detection and diagnosis, but the scope of the studies was limited to behaviors that can only be modeled by the simulation model. In engines, however, there are many parts affected by unknown, complicated physical phenomena. The behavior of sensors installed in such parts cannot be simulated by the SLS model. Half of the sensors used for fault detection and diagnosis measure such physical phenomena. This study suggests a hybrid method that complements the training data with a regression model using sensors that can be modeled by the SLS as explanatory variables and using those that cannot be modeled as response variables.

2. OVERVIEW OF THE RSR ENGINE

2.1. Specification and Operating Conditions

Figures 1 and 2 are a static-firing test and a system diagram of the RSR engine. An expander bleed cycle is employed in the RSR engine, and liquid oxygen (LOX)/liquid hydrogen (LH2) used as the propellant. The fuel turbopump (FTP) and oxidizer turbopump (OTP) are driven by high-temperature hydrogen after cooling a combustion chamber. The pumps in the turbopumps feed LH2 or LOX by rotating each turbine. The RSR engine generated 40 kN at 100% thrust at sea level. Chamber pressure and specific impulse were 3.4 MPa and



Figure 1. Static-firing test of RSR engine.

320 seconds at 100% thrust. This engine was designed for a launch vehicle capable of vertical takeoff and landing. Also, reignition and throttling from 40 to 100% are possible with the opening ratio of flow control valves changing. The static-firing test was conducted over 50 times, and the engine was overhauled a few times during the test campaign.

Figure 3 is the time series of discharge pressure of an inducer and chill-down valve signal. The x-axis is transformed into a range between 0 and 100; 0 and 100 indicate the beginning and end of the sequence respectively. The y-axis is normalized by the min-max normalization. The x-axes and yaxes of all the graphs shown below are transformed by the same way in this paper. The sequence in this case consists of five combustion phases and four chill-down phases. Various sequences were conducted in the test campaign, but this study applies the sequence the test campaign conducted the most often. Figure 4 is a schematic of LH2 flow around the pump. The pump consists of a two-stage centrifugal pump with an inducer and connects with a turbine along an axis, which is a rotating shaft. The red circle marked "Res1" in Fig. 4 indicates the pressure sensor that measures the inducer discharge pressure shown in Fig. 3.

During the combustion phase, LH2 is fed by driving the FTP. Since the main valve opens, the chill-down valve and the bearing chill-down valve close, LH2 is circulated through the bearings by the FTP (Fig. 4 (a)). LH2 flowing through the bearing between the 2nd-stage impeller and the turbine returns to the bearing between the 1st-stage and 2nd-stage impellers through the inside of the hollow shaft. On the other hand, during the chill-down phase, the propellant is moved by only tank pressure because the FTP does not operate. Since the main valve closes, the chill-down valve repeatedly opens and closes, and the bearing chill-down valve opens after engine cutoff, then LH2 flows to cool the pump and bearings (Fig. 4 (b)). Opening and closing the chill-down



Figure 2. System diagram of RSR engine.

valve repeatedly agitates the LH2 in the FTP and cools the pump and bearings effectively. As shown in Fig. 4, the stream of LH2 differs between the combustion and chill-down phases and is greatly affected by the valves.

2.2. Sensors

Engine performance in the static-firing test campaign was measured by over 350 sensors including measurements of ground equipment. This study used 60 sensors mounted on the engine: 26 pressure sensors, 26 thermocouples, four flowmeters, two rotation speed sensors, and two axial displacement sensors for the turbopumps. The system diagram in Fig. 2 indicates the main pipes of the RSR engine. The SLS can simulate the behavior of 30 sensors mounted on these pipes. The sensors that can be modeled by the SLS are listed in Table 1. The remaining 30 sensors, mostly on the turbopumps measured pressure and temperature around the bearings.

The bearings can rotate smoothly while the liquid propellant flows around them. If the propellant is vaporized because of some problem during turbopump operation, the bearings do not work, and severe damage to the turbopumps will result. Res2 and Res3 in Fig. 4 are the thermocouples for monitoring this. Res2 measures the temperature on the outside surface of the bearings, and Res3 measures the temperature of LH2 flowing around the bearings. The developed SLS model cannot simulate the flow indicated by blue arrows in Fig. 4 because flow channels are complicated and, instead, regards the area enclosed by a green box as one pump component. Res1, which measures the discharge pressure of an inducer, is included in the component. Therefore, Res1, Res2, and Res3 cannot be simulated by the SLS model.



(b) Enlarged view of chill-down phase

Figure 3. Time series of discharge pressure of inducer and chill-down valve signal.



(a) Flow of LH2 during combustion phase

(b) Flow of LH2 during chill-down phase



Number	Sensor	Number	Sensor
Exp1	Combustion pressure	Exp16	Volumetric flow rate downstream of OTP
Exp2	Pump discharge pressure of FTP	Exp17	Rotation speed of FTP
Exp3	Pump discharge pressure of OTP	Exp18	Rotation speed of OTP
Exp4	Pressure of mixer at low temperature side	Exp19	Pump discharge temperature of FTP
Exp5	Pressure of mixer at high temperature side	Exp20	Pump discharge temperature of OTP
Exp6	Inlet pressure of regenerative cooling	Exp21	Inlet temperature of regenerative cooling
Exp7	Outlet pressure of regenerative cooling	Exp22	Outlet temperature of regenerative cooling
Exp8	Turbine inlet pressure of FTP	Exp23	Turbine inlet temperature of FTP
Exp9	Turbine outlet pressure of FTP	Exp24	Turbine outlet temperature of FTP
Exp10	Turbine inlet pressure of OTP	Exp25	Turbine inlet temperature of OTP
Exp11	Turbine outlet pressure of OTP	Exp26	Turbine outlet temperature of OTP
Exp12	Pressure of oxidizer side injector	Exp27	Temperature of fuel side injector
Exp13	Pressure of fuel side injector	Exp28	Temperature of oxidizer side injector
Exp14	Volumetric flow rate upstream of FTP	Exp29	Temperature of lower chill-down valve for LH2
Exp15	Volumetric flow rate downstream of FTP	Exp30	Temperature of lower chill-down valve for LOX

Table 1. Sensors that can be modeled by SLS.

3. CREATION OF THE DATASET

3.1. Procedure

Figure 5 is an overview of the procedure for creating the dataset. The first step divides the static-firing test results into results from sensors that can be modeled by the SLS X = $(\mathbf{x}_1, \cdots, \mathbf{x}_{Nx})$ and from those that cannot $\mathbf{Y} = (\mathbf{y}_1, \cdots, \mathbf{y}_{Ny})$. x and y are the time series data of the sensors, and $x_i =$ $(x_i^1, \dots, x_i^T)^t$ and $y_i = (y_i^1, \dots, y_i^T)^t$, respectively. x, y are instantaneous values of the time series data, and subscript $i \in$ [1, Nx], $j \in [1, Ny]$, and superscript $t \in [1, T]$ are the number of $X = \mathbb{R}^{T \times Nx}$, $Y = \mathbb{R}^{T \times Ny}$, and time, respectively. To train the regression model, X and Y are used as the explanatory variable and response variable. Then, M explanatory variables $(\tilde{X}^1, \dots, \tilde{X}^M)$ are created by the developed SLS model $g(\boldsymbol{\theta})$ with $\boldsymbol{\Theta} = (\boldsymbol{\theta}^1, \cdots, \boldsymbol{\theta}^M)$. $\boldsymbol{\Theta}$ is created by the Monte-Carlo method based on model parameter $\boldsymbol{\theta}$, fitted to the static-firing test results with data assimilation (Sato et al., 2019). M response variables $(\widetilde{Y}^1, \dots, \widetilde{Y}^M)$ are obtained by the trained regression model $f(\mathbf{X})$. Finally, by combining $(\widetilde{\mathbf{X}}^1, \cdots, \widetilde{\mathbf{X}}^M)$ and $(\widetilde{\mathbf{Y}}^1, \cdots, \widetilde{\mathbf{Y}}^M)$, the dataset $\mathcal{D} = \left(\left(\widetilde{X}^1, \widetilde{Y}^1 \right), \cdots, \left(\widetilde{X}^M, \widetilde{Y}^M \right) \right)$ is obtained.

This study uses 24 cases out of over 50 cases of static-firing test results to train the regression model, and the gross number of T is approximately 650,000. The test data for the regression model is the time series shown in Fig. 3, and its T is approximately 30,000. Nx is 41 consisting of the 30 sensors listed in Table 1 and signals of valves, and Ny has three members: Res1, Res2, and Res3 shown in Fig. 4.

3.2. Regression Model

The sequence in Fig. 3 is strongly affected by the valve behavior. The flow direction around the pump in Fig. 4 is different between the combustion and chill-down phases as well. Res2 in Fig. 4 measures the temperature of the outside surface of the bearing, not the fluid temperature. Res3 measures the fluid temperature after it flows through the impellers and complicated channels, and it is affected by heat transfer from thermal mass especially during the chill-down phase. This study mainly aims to investigate whether the regression model can complement the dataset using a simple linear regression model, Ridge regression, but plans on using a nonlinear regression model to improve the prediction accuracy further.

3.3. Clustering for Time-Varying Operating Conditions

The main purpose of the static-firing test campaign was to determine an operating point that would allow the engine to operate normally. Therefore, this increases the amount of data for the combustion phase. Even if a nonlinear regression model is used, the usual regression models tend to value the major phase having the most data. Although a minor phase with a limited amount of data tends to be neglected, it is ideal for practicing fault detection and diagnosis for sequences that include both the major and minor phases. To prevent any bias caused by a difference in the amounts of data and the physical phenomena shown in Fig. 4, X is divided into clusters in advance, and regression models are individually trained on each clustered X. The procedure for a training regression model is shown in Fig. 6.

Initially, the static-firing test results are divided into training and test data, and X of the training data is divided into Nc

clusters. This study uses the Gaussian Mixture Model (GMM) as a clustering method as follows:

$$p(x) = \sum_{c=1}^{Nc} \pi_c \mathcal{N}(x | \boldsymbol{\mu}_c, \boldsymbol{\Sigma}_c) \qquad (1)$$
$$\sum_{c=1}^{Nc} \pi_c = 1 \qquad (2)$$

where, *Nc* is 20 and $c \in [1, Nc]$. The number of supposed phases according to operating conditions in the training data was around 20, so this study uses only *Nc*=20. Mixture weight π_c , mean vector $\boldsymbol{\mu}_c$, and covariance matrix $\boldsymbol{\Sigma}_c$ are obtained by the EM algorithm.

Then, **Y** is also divided into *Nc* clusters by label $L = (l_1, \dots, l_T)^t$ from the GMM, and the regression models are trained from the thus obtained clusters. The regularization parameter of the Ridge regression model is obtained when the R2 score is maximum in 5-fold cross validation. \tilde{Y}_c is calculated by inputting X_c divided by the GMM into the regression models trained on each cluster. Finally, the performance of the clustered regression models is evaluated by comparing the merged \tilde{Y} with Y of the test data and evaluates it with the Root Mean Square Error (RMSE) as follows:



Figure 5. Overview of procedure for creating dataset.

$$RMSE = \sqrt{\frac{\Sigma(\mathbf{y} - \widetilde{\mathbf{y}})^2}{n}}$$
(3)

where *n* is the number of data.

4. PREDICTION RESULTS AND DISCUSSION

4.1. Prediction without Clustering

Figure 7 is the comparison between the static-firing test results and predictions of the Ridge regressor without clustering X of the test data. The prediction of Res1 shown in Fig. 7 (a) generally agrees with the static-firing test results. Focusing on the area enclosed by a red box in Fig. 7 (a), however, the chill-down phase indicated by B and the



switching point of the phases indicated by T1 and T2 are not predicted well, as can be seen from Fig. 7(b). Since Res1 (see Fig. 4) is the sensor that measures the inducer discharge pressure, its behavior is similar to the rotation speed, the discharge pressure of the turbopump, and flow rate during the combustion phase. The behavior of other pressure sensors is also similar, so the prediction accuracy for Res1 is improved because such sensors are used as the explanatory variables for the regression models. Moreover, since a large number of data for the combustion phase is included in the test data as well, the training regression model values this phase.

On the other hand, LH2 is fed by only tank pressure because the turbopump is stopped during the chill-down phase. The



Figure 7. Comparison between static-firing test results and prediction of Ridge regressor without clustering.

main valve closes, so its upstream fluid is strongly affected by the chill-down valve, but its downstream fluid is not affected. There are a few sensors whose behavior resembles that of Res1 during the chill-down phase. The number of data for the chill-down phase is smaller than that for the combustion phase, and the behaviors (such as valve operation) is different between the combustion and chilldown phases. The training regression model is inadequate for the above reasons.

Considering the prediction result for Res1, the regression model does not predict the behavior of the temperature Res2 and Res3 well. Some peaks are observed in the prediction results during the chill-down phase, so it is found that predicting the behavior of thermocouples is more difficult than the pressure sensor. When the turbopump is stopped and the propellant is stilled, the thermocouples are affected by heat from the outside and residual heat in the heat mass, such as pipes and pumps. The physical phenomena that affects the sensor behavior is the difference between the combustion and chill-down phases. Since the main valve closes during the chill-down phase, the explanatory variables for the behavior around the pump are limited. The chill-down phase behavior cannot be predicted by the regression model that values fitting the combustion phase.

4.2. Prediction with Clustering

Figure 8 is a comparison between the static-firing test results and prediction by the Ridge regressors with clustering X of the test data. The gray curves indicate the static-firing test result, and the colored curves indicate the prediction result. The color is changed for each cluster according to the legend at the top of Fig. 8 and common in Fig. 8. Note that clusters 1-4 expressed by the similar blue in Fig. 8 (b) are different. Although only four clusters are indicated here to distinguish the similar blue clusters, this sequence consists of more than four clusters as shown in Fig. 8. Focusing on the divided points of each cluster, the sequences are divided according to the steady state, transient state, and valve operation. The RMSE of the prediction results are listed in Table 2. All the response variables are improved by clustering.

Figure 8 (a) shows that the prediction result for Res1 agrees with the static-firing test result. As shown in Fig. 8 (b), an enlarged view of the area enclosed by the red box in Fig. 8 (a), the prediction accuracies for the switch of phases and the chill-down phase are improved. By individually training the regression models on each cluster, the minor chill-down phase had a small number of data and the major combustion phase had a large number of data, and were both valued in training the regression model. Switching the regression models predicts response variables well even if the physical phenomenon and the explanatory variable of each phase are different. As shown in Fig. 7 (b)-(f), the prediction results for Res2 and Res3 do not fit the static-firing test results even in the combustion phase, however, the accuracies of Res2 and Res3 in Fig. 8 (b)-(f) are also improved by clustering. Focusing on the chill-down phase in Fig. 8 (d), the peaks shown in Fig. 7 (c) are prevented and the tendency of the prediction result is improved, but the prediction accuracy is worse than for Res1. On the other hand, the prediction result

Table 2. RMSE of prediction result.

Company	RMSE		
Sensor	without clustering	with clustering	
Res1	0.01320	0.003709	
Res2	0.7764	0.4459	
Res3	0.9447	0.4386	

for Res3 shown in Fig. 8 (e) generally fits the static-firing test result and it can predict not only the steady state during the combustion phase but also transient states, such as startup and cutoff. The chill-down phase is also predicted accurately, as shown in Fig. 8 (f). As mentioned in Section 2.2, the measurement point of Res3 differs from that of Res2. As shown in Fig. 4, Res2 measures the outside surface temperature of the bearing, which is changed by the heat transfer from LH2 and the bearing friction, not the fluid temperature. The temperature change at Res3 is based more on simple physical phenomena than is Res2, so the prediction accuracy for Res3 is better than Res2.

One method to improve the prediction accuracy for Res2 is to change the clustering method. Before training the regression model, X is divided into clusters by the GMM in order to reduce the bias that values a major phase with a large number of data. However, since the number of the clusters is a hyper-parameter of the GMM, there is the possibility that a minor phase with a small number of data could be classified in a neighboring cluster of a major phase, depending on the set cluster number. For the static-firing test result indicated by the gray curve in Fig. 8 (c), the temperature in the combustion and chill-down phases both gradually decrease. Although the tendency of the first chill-down phase particularly differs from the fourth, the GMM classifies them into the same cluster. Since the tendencies between phases in Res1 and Res3 are almost the same, the prediction accuracy for Res2 seems to be improved by dividing the first chilldown phase as another cluster. Another method to improve the prediction accuracy for Res2 is to apply a nonlinear regression model. As mentioned above, since the Res2 is based on complicated physical phenomena, a linear regression model has trouble predicting such behavior. The linear regression model can predict the phase based on comparably simple physical phenomena, such as the combustion phase, so switching a linear and a nonlinear regression model according to each phase is effective in improving prediction accuracy.

5. CONCLUSION

For fault detection and diagnosis with machine learning, training data needs to be created for time-varying operating conditions. The authors have developed a system-level simulator that reasonably represents the global behavior of a reusable rocket engine. However, there are components that cannot be modeled by the system-level simulation, and they are also the targets of fault detection and diagnosis. The regression model was developed to complement the training data. Its explanatory variables are the sensors that can be modeled by the system-level simulation, and its response variables are the ones that cannot be modeled. The sequences of the reusable rocket engine consist of the various operating conditions, such as the combustion and chill-down phases. Training the regression model usually focuses on a major phase represented by a large amount of data, so a regression model based on the major phase tends to neglect a minor phase having a small number of data. Moreover, physical phenomena can change drastically between phases according to changes in the flow field inside pipes and turbopumps and in valve behavior. To solve such issues, the explanatory variables are divided into clusters by the Gaussian mixture model. The Ridge regression model trained on each cluster predicts the static-firing test results complied under various operating conditions well. From the above, the present method is shown to combine system-level simulation and the regression model used to generate training data for fault detection and diagnosis. However, the prediction accuracies for some sensor behavior are insufficient. Since nonlinear phenomena are dominant in a reusable rocket engine, improving prediction accuracy by applying a nonlinear regression model will be valuable work for the future.



Figure 8. Comparison between test results and prediction of Ridge regressor with clustering.

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