

# Adaptive Res-LSTM Attention-based Remaining Useful Lifetime Prognosis of Rolling Bearings

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## ABSTRACT

Predicting the Remaining Useful Lifetime (RUL) of bearings is crucial for the maintenance and reliability of rotating machinery. This paper presents a novel approach utilizing PRONOSTIA and XJTU-SY datasets for RUL prediction. The proposed methodology leverages Synchrosqueezing Wavelet Transform (SSWT) and Random Projection (RP) to extract significant features from vibration signals. These features are then fed into a Residual Network (ResNet) combined with a temporal attention layer, followed by a Long Short-Term Memory (LSTM) model, referred to as the Adaptive Residual Attention LSTM (ARAL), to assess the Health Indicator (HI) of the bearings. Notably, an exponential data labeling technique is employed instead of traditional linear labeling, enhancing the robustness of the HI assessment. Following the HI estimation, the three-sigma method is applied to identify the degradation starting point. Subsequently, Gaussian Process Regression (GPR) is utilized to predict the RUL from this point forward. The proposed method demonstrates superior performance compared to existing techniques, providing more accurate and reliable RUL predictions. Experimental results show that this integrated approach effectively captures the complex degradation patterns of bearings, making it a valuable tool for prognostics and health management in industrial applications.

## 1. INTRODUCTION

Rolling bearings are critical components in mechanical equipment, with their degradation directly impacting overall stability and safety. Degradation in bearings is often caused by multiple mechanisms, including wear, fatigue, and microfractures in materials, which develop under fluctuating loads and unstable operating conditions. These phenomena can com-

pound over time, leading to more severe damage and eventual failure. Early fault detection and accurate prediction of their RUL are essential for optimizing maintenance, preventing accidents, and enhancing efficiency. Manual monitoring in such complex conditions is ineffective. With the rise of artificial intelligence, Prognostics and Health Management (PHM) has emerged as a vital field, yielding significant research and practical applications (X. Li, Yu, Lei, Li, & Yang, 2024; Ding et al., 2023; Suh, Lukowicz, & Lee, 2022).

To estimate rolling bearing RUL, both model-based and data-driven methods are commonly employed. Model-based methods aim to develop a physical model describing the degradation trend of the mechanical system or component (Londhe, Arakere, & Subhash, 2017; Qin, Xiang, Chai, & Chen, 2020). However, creating such models for complex equipment under varying conditions is challenging and limits their applicability. Conversely, data-driven methods use machine learning and deep learning technologies to analyze measurement data and uncover the dynamic characteristics of mechanical systems (Que & Xu, 2019).

Data-driven prognostics methods generally follow a three-step framework: data acquisition, HI construction, and RUL prediction (Lei et al., 2018). The HI in bearings serves as an abstract measure of the overall health or degradation status of the bearing. It is derived from features extracted from vibration signals that reflect the bearing's condition. The accuracy of RUL prediction is highly dependent on the HI construction phase, making the extraction of meaningful features from measured signals a critical challenge. A well-constructed HI, based on high-quality features, can efficiently track bearing degradation (Zhang, Tang, Han, & Deng, 2017).

Historically, bearing fault diagnosis and RUL prediction have relied on signal processing techniques such as Wavelet Packet Decomposition (WPD) and Empirical Mode Decomposition (EMD), which effectively extract features from vibration signals. However, these methods often struggle with non-stationary

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signals and noise, limiting their accuracy and applicability.

With advancements in sensing technology and computer science, big data-driven deep learning has become a powerful tool for autonomously extracting valuable features from extensive datasets. This approach has garnered significant attention in rolling bearing RUL prediction. For instance, time-frequency features, reduced in dimensionality, have been employed as inputs to multi-scale Convolutional Neural Networks (CNN) for assessing the remaining life of rolling bearings (Zhu, Chen, & Peng, 2019a). Other studies have proposed LSTM networks utilizing frequency domain features for RUL prediction of gears (Yan, Qin, Xiang, Wang, & Chen, 2020). Additionally, multi-technique prognostic approaches integrating multiple machine learning and deep learning models have been developed for RUL prediction (L. Li, Xu, & Li, 2023), while 2D Time-Scale (TS) images generated by Continuous Wavelet Transform (CWT) have been used as inputs for 2D CNNs to develop health indicators for predicting the remaining life of bearings (Yoo & Baek, 2018). Despite these advancements, many deep learning models still struggle with the vanishing gradient problem, which hampers the training of deep networks and limits their ability to capture complex patterns in the data.

Attention mechanisms (Vaswani et al., 2023), which can associate different parts of a sequence to create a distinctive representation, have gained success in diverse applications such as natural language processing, computer vision, and RUL prediction (Deng et al., 2023). These mechanisms function by establishing relationships between features from different points in the sequence, assigning varying levels of importance to these features, which helps to highlight critical information while downplaying less relevant data. By integrating a temporal attention mechanism, it becomes possible to effectively extract significant degradation signals from sensor data, while minimizing the impact of irrelevant information.

Building on these advancements, the SSWT and RP have shown great promise in our previous research on bearing fault diagnosis by capturing Time-Frequency (TF) information and reducing feature dimensionality, leading to better accuracy (Najdi, Benbrahim, & Kabbaj, 2024). SSWT (Daubechies, Lu, & Wu, 2011) provides precise localization of signal features, enhancing the detection of subtle changes. RP reduces computational complexity while retaining essential information from high-dimensional data (Achlioptas, 2003), addressing key limitations of traditional methods in non-stationary environments.

To address existing deep learning limitations, this paper proposes ARAL, a novel approach integrating a ResNet-based CNN, a temporal attention layer, and an LSTM network. This combination enhances feature extraction and improves RUL prediction accuracy. ResNet CNNs mitigate the vanishing gradient problem (Shah, Kadam, Shah, & Shinde, 2016), en-

abling deeper network training and complex feature extraction from vibration signals. The attention mechanism highlights the most relevant input data, and the LSTM network captures temporal dependencies, effectively modeling the data's sequential nature.

The main contributions of this research are the following:

- **Enhanced Feature Extraction:** Leveraging SSWT and RP to effectively capture and reduce the dimensionality of significant features from vibration signals, addressing key limitations of traditional methods.
- **Novel Health Indicator:** Introducing ARAL, combining a ResNet-based CNN, a temporal attention layer, and an LSTM network to improve the accuracy of HI assessments and RUL predictions by mitigating the vanishing gradient problem and capturing complex temporal dependencies.
- **Exponential Data Labeling:** Utilizing an exponential data labeling technique for more robust HI assessment and applying GPR following a three-sigma method to predict RUL, demonstrating superior performance in capturing complex degradation patterns and providing reliable RUL predictions.

The rest of the paper is structured as follows: Section 2 presents the theoretical framework of the proposed RUL estimation method. Section 3 details the experimental validation and results analysis using two bearing datasets. Finally, Section 4 provides the conclusion.

## 2. THE PROPOSED METHOD FOR RUL PREDICTION

### 2.1. The SSWT-RP Signal Transformation

The SSWT (Daubechies et al., 2011) is an advanced TF analysis method that enhances the concentration of a signal's energy in the Time-Frequency plane while preserving the time resolution. Given a signal  $s(t)$ , the CWT of  $s(t)$  at scale  $a$  and time  $t$  is defined as (Sadowsky, 1994):

$$W_{\psi}s(a, t) = \frac{1}{\sqrt{a}} \int_{-\infty}^{\infty} s(\tau)\psi^* \left( \frac{\tau - t}{a} \right) d\tau \quad (1)$$

From the CWT, the instantaneous frequency (IF)  $\omega_s(a, t)$  is derived as:

$$\omega_s(a, t) = \frac{1}{2\pi j} \frac{\partial}{\partial t} (\ln W_{\psi}s(a, t)) \quad (2)$$

The SSWT then refines the CWT by reassigning its coefficients from the Time-Scale plane  $(t, a)$  to the Time-Frequency plane  $(t, \omega_s(a, t))$ , effectively mapping:

$$SSWT s(t, \xi) = \int_0^\infty W_\psi s(a, t) \delta(\xi - \omega_s(a, t)) \frac{da}{a^{5/2}} \quad (3)$$

where  $\xi$  represents the reassigned frequency. This process results in a TF matrix  $SSWT s(t, \xi)$ , which provides a clearer and more concentrated representation of the signal's energy distribution over time and frequency.

Transforming big signals to TF can result in some redundancy in the representation which will be cumbersome for processing. To reduce the dimensionality of the TF matrix while preserving its essential features, we apply RP. Let the TF representation obtained from SSWT be  $X \in \mathbb{R}^{m \times n}$ , where  $m$  is the number of time points and  $n$  is the number of frequency bins. In RP, the original high-dimensional data  $X$  is projected into a lower-dimensional space using a randomly generated matrix  $R \in \mathbb{R}^{k \times n}$ , where  $k \ll n$ :

$$Y = X \cdot R^T \quad (4)$$

Here,  $Y \in \mathbb{R}^{m \times k}$  is the reduced-dimensionality representation of the TF matrix. The elements of  $R$  are chosen to be independent and identically distributed (i.i.d.) and scaled to unit length. This projection approximately preserves the distances between the original data points, as guaranteed by the Johnson-Lindenstrauss lemma (Johnson & Lindenstrauss, 1984):

$$(1 - \epsilon) \|X_i - X_j\|^2 \leq \|Y_i - Y_j\|^2 \leq (1 + \epsilon) \|X_i - X_j\|^2 \quad (5)$$

for any  $0 < \epsilon < 1$  and for all pairs of data points  $X_i, X_j$  in the original high-dimensional space.

The resulting matrix  $Y$  retains the most significant information from the original TF representation but in a much lower-dimensional space, making it suitable for subsequent processing tasks such as classification or regression.

## 2.2. ARAL

The input matrix from the SSWT-RP method is denoted as  $Y \in \mathbb{R}^{H \times W}$ , where  $H$  is the height and  $W$  is the width. The convolutional layer applies a set of filters (kernels) to  $Y$  to produce feature maps, as shown in Figure 1. Let  $K \in \mathbb{R}^{k_H \times k_W \times F}$  be the filter, where  $k_H$  and  $k_W$  are the height and width of the filter, and  $F$  is the number of filters. The output  $Y' \in \mathbb{R}^{H' \times W' \times F}$  is computed as:

$$Y'_{h', w', f} = \sum_{i=1}^{k_H} \sum_{j=1}^{k_W} K_{i, j, f} \cdot Y_{h'+i-1, w'+j-1} \quad (6)$$

where  $H'$  and  $W'$  are the height and width of the output feature map from the convolutional layer, determined by the strides and padding.

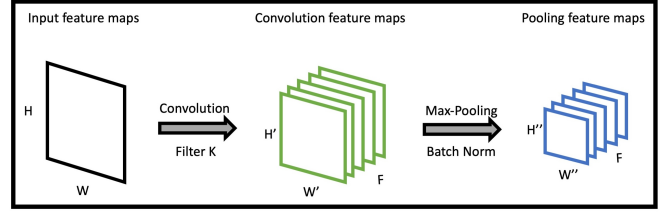


Figure 1. Convolution and pooling.

Next, Batch Normalization (BN) is applied to the output of the convolutional layer to achieve zero mean and unit variance, followed by scaling and shifting. Let  $\hat{Y}$  be the normalized output:

$$\hat{Y}'_{h', w', f} = \gamma_f \left( \frac{Y'_{h', w', f} - \mu_f}{\sqrt{\sigma_f^2 + \epsilon}} \right) + \beta_f \quad (7)$$

where  $\mu_f$  and  $\sigma_f^2$  are the mean and variance of the feature map  $f$ ,  $\gamma_f$  and  $\beta_f$  are learnable parameters, and  $\epsilon$  is a small constant added for numerical stability.

The ReLU activation function introduces non-linearity:

$$\tilde{Y}'_{h', w', f} = \max(0, \hat{Y}'_{h', w', f}) \quad (8)$$

MaxPooling reduces the spatial dimensions (height and width) of the feature maps by taking the maximum value over a pooling window:

$$P_{h'', w'', f} = \max_{(i, j) \in \text{pool\_window}} \tilde{Y}'_{h'+i, w'+j, f} \quad (9)$$

where  $h''$  and  $w''$  are the new height and width after pooling, and  $s_h$  and  $s_w$  are the strides.

The output from the MaxPooling layer,  $P$ , is then fed into a series of Residual Blocks (ResBlock), as illustrated in Figure 2. Each ResBlock consists of two convolutional layers with an identity shortcut connection. For each block  $k$ :

$$U_k = \text{Conv}(P, F_k, (k_H, k_W), \text{stride}) \quad (10)$$

$$U_k = \text{BatchNormalization}(U_k) \quad (11)$$

$$U_k = \text{ReLU}(U_k) \quad (12)$$

$$U_k = \text{Conv}(U_k, F_k, (k_H, k_W), (1, 1)) \quad (13)$$

$$U_k = \text{BatchNormalization}(U_k) \quad (14)$$

If the input dimensions differ from the output dimensions, we

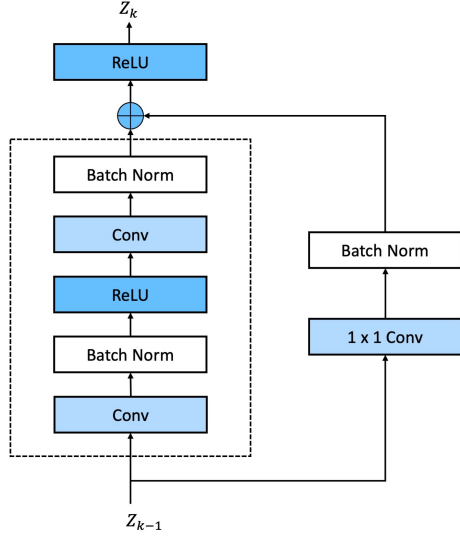


Figure 2. ResNet block.

perform a  $1 \times 1$  convolution and BN on the identity mapping:

$$X_{\text{shortcut}} = \text{Conv}(P, F_k, (1, 1), \text{stride}) \quad (15)$$

$$X_{\text{shortcut}} = \text{BatchNormalization}(X_{\text{shortcut}}) \quad (16)$$

Add the shortcut:

$$Z_k = \text{ReLU}(U_k + X_{\text{shortcut}}) \quad (17)$$

The final output  $Z_k$ , denoted as  $Z_k \in \mathbb{R}^{H \times W \times F}$ , of the Res-Block is then passed to the attention block, as illustrated in Figure 3.

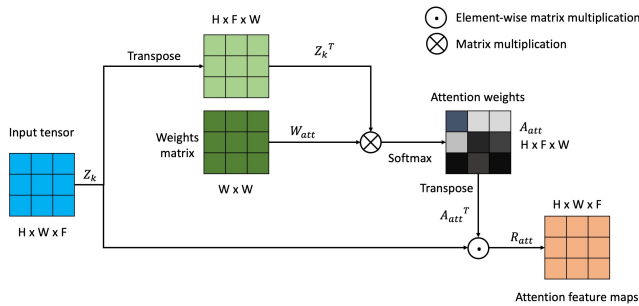


Figure 3. Temporal Attention block.

The attention mechanism starts by computing the attention weights. First, the input tensor  $Z_k$  is transposed and then multiplied by the weight matrix  $W_{\text{att}}$ . The attention mechanism assigns different weights to different time steps of the input tensor. The softmax function is applied to obtain the attention weights:

$$A_{\text{att},h,f,w} = \frac{\exp\left(\sum_j (Z_k)_{h,j,f}^T \cdot W_{\text{att},j,w}\right)}{\sum_k \exp\left(\sum_j (Z_k)_{h,j,f}^T \cdot W_{\text{att},j,k}\right)} \quad (18)$$

The final output of the attention layer is then calculated by performing an element-wise multiplication between the original input  $Z_k$  and the attention weights:

$$R_{\text{att}} = Z_k \odot A_{\text{att}}^T \quad (19)$$

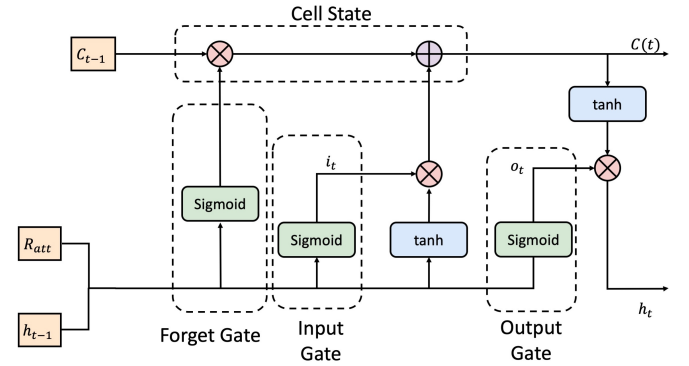


Figure 4. The LSTM architecture.

The LSTM layer processes the sequence data returned by the attention layer, capturing temporal dependencies, as represented in Figure 4. The LSTM equations are defined for each time step  $t$  as follows:

- Input gate:  $i_t = \sigma(\mathbf{W}_i R_{\text{att},t} + \mathbf{U}_i h_{t-1} + \mathbf{b}_i)$
- Forget gate:  $f_t = \sigma(\mathbf{W}_f R_{\text{att},t} + \mathbf{U}_f h_{t-1} + \mathbf{b}_f)$
- Cell state:  $c_t = f_t \otimes c_{t-1} + i_t \otimes \tanh(\mathbf{W}_c R_{\text{att},t} + \mathbf{U}_c h_{t-1} + \mathbf{b}_c)$
- Output gate:  $o_t = \sigma(\mathbf{W}_o R_{\text{att},t} + \mathbf{U}_o h_{t-1} + \mathbf{b}_o)$

where  $\sigma(z) = \frac{1}{1+e^{-z}}$  is the sigmoid function.

Finally, the output of the LSTM layer is calculated as follows:

$$h_t = o_t \otimes \tanh(c_t) \quad (20)$$

### 2.3. RUL prediction based on SSWT-RP-ARAL

In this section, we present the deep learning-based methodology for RUL prediction using SSWT, RP, and a combination of ResNets, Temporal Attention Block, and LSTM models. The procedure is shown in Figure 5 and comprises three stages: data preparation, HI construction, and RUL estimation. In the data preparation stage, vibration signals are transformed into TF domain features using SSWT, then dimensionality is reduced using RP. In the HI construction stage,

these features build the training and testing datasets. ResNet extracts deep features, the Temporal Attention Block enhances relevant temporal information, and LSTM captures temporal dependencies, training the model to estimate the HI values. In the RUL estimation stage, the three-sigma rule identifies the abnormal degradation point, and GPR predicts the future HI and degradation trends. The RUL is then calculated as the time difference between the HI reaching a threshold and the current time.

### 2.3.1. Health indicator constructed by SSWT-RP-ARAL

#### (i) Architecture of the ARAL-HI model

The architecture of the ARAL-HI model, presented in the Figure 6, consists of multiple stages that process the input data to construct health indicators. The initial stages involve the SSWT-RP transformed input  $Y$ , which is passed through the convolutional and ResBlocks, followed by the attention mechanism and LSTM layers. The final output of the LSTM layers serves as the input to a series of dense layers designed to further refine the health indicators.

After the LSTM layers, the output  $h_t$  is fed into one or more fully connected (dense) layers. These dense layers are equipped with dropout regularization to prevent overfitting. Let  $D$  be the dropout rate, and  $W_d$  and  $b_d$  be the weights and biases of the dense layers, respectively. The dense layer operation can be expressed as:

$$d_t = \text{Dropout}(\text{ReLU}(W_d h_t + b_d), D) \quad (21)$$

Following the dense layers, a final dense layer with a sigmoid activation function is applied to produce the HIs. The sigmoid layer converts the output into a value between 0 and 1, indicating the health state of the bearing. Let  $W_s$  and  $b_s$  be the weights and biases of the sigmoid layer. The health indicator  $HI_t$  is computed as:

$$HI_t = \sigma(W_s d_t + b_s) \quad (22)$$

The resulting  $HI_t$  represents the normalized health state at time step  $t$ , providing a comprehensive view of the bearing's condition over time.

#### (ii) Exponential Data labeling

Instead of using the conventional linear data labeling of the run-to-failure data, an exponential function is used to reflect the bearing defect progression over time. The exponential labeling function is defined as:

$$\text{HealthLabel}(t) = \frac{\exp(\alpha \cdot x) - 1}{\exp(\alpha) - 1} \quad (23)$$

where  $x = \frac{t}{T}$ ,  $t$  is the current time step,  $T$  is the total time steps until failure, and  $\alpha$  is the scaling factor. An example is shown in the Figure 7, where we construct the health label of the Bearing1\_3. The scaling factor is chosen based on the best RMSE value of the training, with the scaling factors of 1.3 and 1.5 being tested, and 1.3 yielding the best results. Each time step  $t$  in the dataset is assigned a label  $\text{HealthLabel}(t)$  using this exponential function, providing a more realistic representation of the bearing's degradation process.

#### (iii) Model Training

The network is trained using the labeled dataset, with the objective of minimizing the difference between the predicted health indicators and the true health labels. The training process includes forward propagation through the convolutional, residual, attention, LSTM, dense, and dropout layers, followed by a sigmoid activation function to produce the final HIs.

The loss function used to evaluate the model's performance is the RMSE, which is defined as:

$$\text{RMSE} = \sqrt{\frac{1}{N} \sum_{i=1}^N (\widehat{HI}_i - HI_i)^2} \quad (24)$$

where  $\widehat{HI}_i$  is the predicted health indicator,  $HI_i$  is the true health indicator, and  $N$  is the total number of samples. The RMSE function measures the square root of the average squared differences between the predicted and true values.

The training process involves minimizing the RMSE by adjusting the model's parameters through backpropagation and Adam optimizer. This ensures that the predicted health indicators closely match the true health indicators, improving the model's prediction accuracy.

### 2.4. RUL estimation

The calculation of the RUL involves several key steps, each underpinned by important theoretical concepts:

#### 2.4.1. Smoothing the HI Curve

Once the HI curve is obtained from the SSWT-RP-ARAL model, we first apply a smoothing technique to reduce noise and highlight the underlying degradation trend. The smoothing is done using a Moving Average (MA), which helps to smooth out short-term fluctuations and reveal the long-term trend in the HI data. The moving average is defined as:

$$\text{MA}(t) = \frac{1}{2k+1} \sum_{i=-k}^k HI(t+i) \quad (25)$$

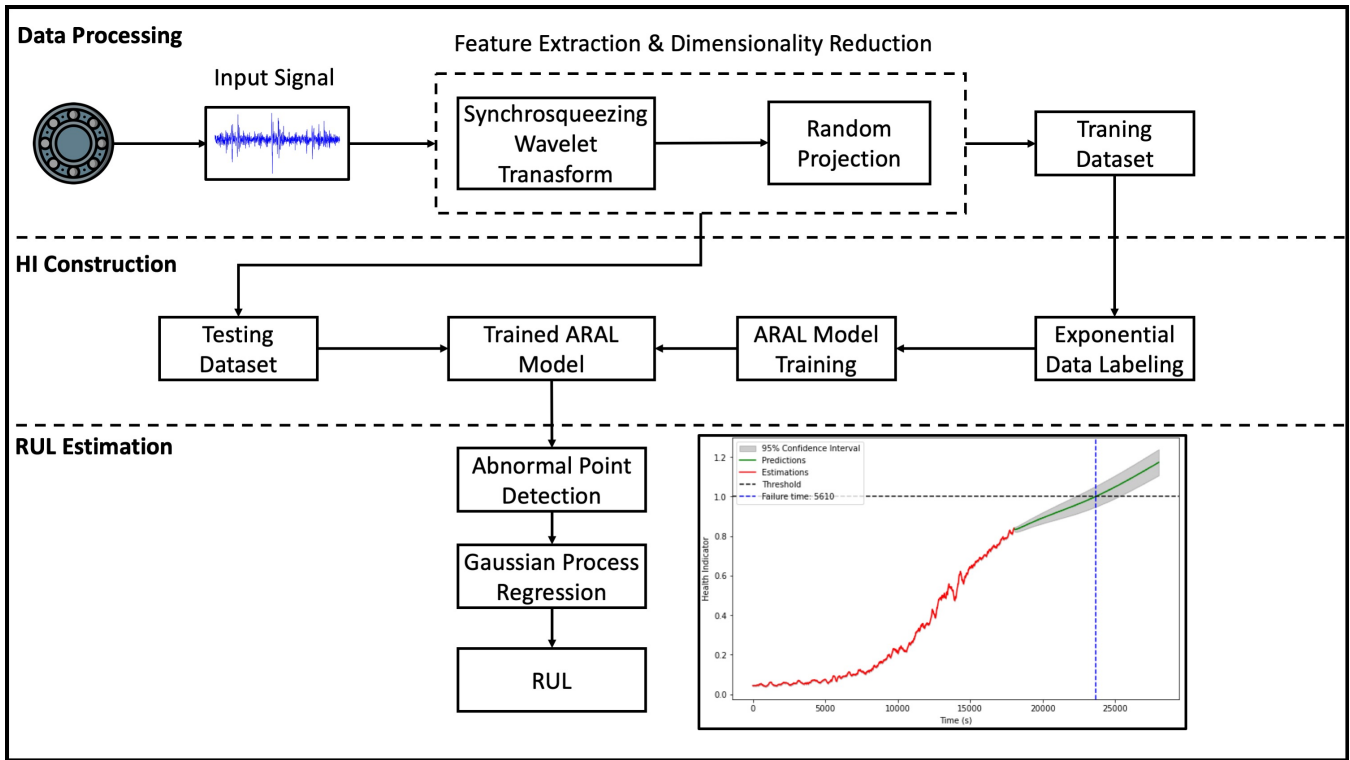


Figure 5. Framework of the proposed SSWT-RP-ARAL Method for RUL Prognosis.

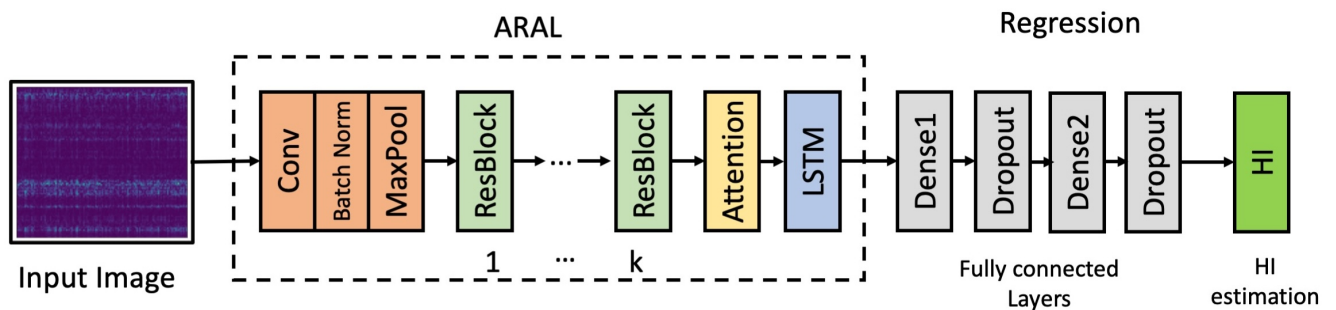


Figure 6. Architecture of the ARAL health assessment model.

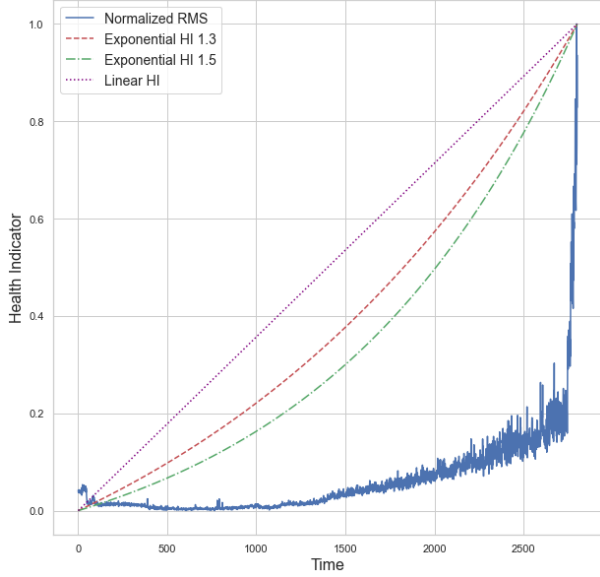


Figure 7. Exponential Labeling vs Linear Labeling.

where  $MA(t)$  is the moving average at time  $t$ , and  $k$  is the window size for the MA.

#### 2.4.2. Detecting the Abnormal Point with 3-Sigma Method

To identify the point at which abnormal degradation starts, we use the 3-Sigma method. This statistical method detects points that deviate significantly from the mean of the smoothed HI curve. The mean  $\mu$  and standard deviation  $\sigma$  of the smoothed HI data are calculated, and any point  $HI(t)$  that satisfies the condition:

$$|HI(t) - \mu| > 3\sigma \quad (26)$$

is considered an abnormal point. The time corresponding to the first detected abnormal point is denoted as  $T_a$ . This point marks the beginning of significant degradation, and subsequent analysis focuses on the HI data from this point onward.

#### 2.4.3. GPR model

To predict the future degradation and estimate the RUL, we fit a GPR model to the HI data from the abnormal point  $T_a$  to the current observation time  $T_s$ . GPR is a non-parametric, Bayesian approach that provides both a prediction and an uncertainty estimate. The GPR model is defined by a mean function  $m(t)$  and a covariance function  $k(t, t')$ :

$$HI(t) \sim \mathcal{GP}(m(t), k(t, t')) \quad (27)$$

A combination of long and short term trend kernels allows the GPR model to capture various patterns and noise characteristics in the HI data.

#### 2.4.4. RUL calculation

To calculate the RUL, we extrapolate the GPR model to predict the HI values until the HI reaches a failure threshold  $HI_{th}$ . The predicted time  $T_f$  at which the HI curve intersects the threshold is determined, and the RUL is calculated as the difference between  $T_f$  and the current observation time  $T_s$ :

$$RUL(T_s) = T_f - T_s \quad (28)$$

In practice, the RUL prediction process is detailed in Algorithm 1:

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#### Algorithm 1 RUL Prediction via SSWT-RP-ARAL Method

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- 1: **Input:** Vibration signals  $s(t)$  for bearings  $i = 1$  to  $N$
  - 2: **Output:** RUL estimation
  - 3: **Stage 1: Data Preparation**
  - 4: **for**  $i = 1$  to  $N$  **do**
  - 5:     Transform  $s_i(t)$  to TF domain using SSWT, resulting in  $X_i$
  - 6:     Apply RP to  $X_i$  to obtain  $Y_i$
  - 7: **end for**
  - 8: **Stage 2: HI Construction and Training**
  - 9: **for**  $i = 1$  to  $N$  **do**
  - 10:     Label data with exponential function to create  $HealthLabel(t)$
  - 11:     Initialize  $F_i = Y_i$
  - 12:     **for**  $k = 1$  to  $K$  **do**
  - 13:         Pass  $F_i$  through ResNet Block  $k$ , updating  $F_i$
  - 14:     **end for**
  - 15:     Apply Temporal Attention to  $F_i$ , yielding  $A_i$
  - 16:     Pass  $A_i$  through LSTM layers to obtain  $h_{i,t}$
  - 17:     Feed  $h_{i,t}$  into Dense layers with Dropout, producing  $d_{i,t}$
  - 18:     Compute predicted  $\widehat{HI}_{i,t}$  using Sigmoid activation on  $d_{i,t}$
  - 19: **end for**
  - 20: Train model by minimizing RMSE between  $\widehat{HI}_{i,t}$  and  $HealthLabel(t)$  using Adam optimizer
  - 21: **Stage 3: RUL Estimation**
  - 22: **for**  $i = 1$  to  $N$  **do**
  - 23:     Smooth HI curve with MA to obtain  $MA(t)$
  - 24:     Detect first abnormal point  $T_{a,i}$  using 3-Sigma method on  $MA(t)$
  - 25:     Fit GPR model on HI data from  $T_{a,i}$  to current time  $T_s$
  - 26:     Calculate RUL as the time difference when  $MA(t)$  reaches failure threshold
  - 27: **end for**
  - 28: **Return** RUL for each bearing  $i$
- 

### 3. THE EXPERIMENTAL VALIDATION

To demonstrate the effectiveness and advantages of the proposed method for predicting the RUL of bearings, two renowned public datasets were utilized: the PRONOSTIA dataset (Nectoux et al., 2012) and the XJTU-SY dataset (Wang, Lei, Li, & Li, 2020a). The PRONOSTIA dataset, consisting of run-to-failure vibration signals from bearings, was employed to evaluate the performance of our method against several established techniques. Additionally, the XJTU-SY dataset, which provides comprehensive data on bearing degradation under varying operational conditions, was used to further validate our method's prediction capabilities. Benchmarking against various state-of-the-art techniques highlighted the predictive accuracy and robustness of our approach.

### 3.1. Case study 1: IEEE-PHM-2012-Challenge

#### 3.1.1. Experimental setup and evaluation metrics

The PRONOSTIA dataset, part of the IEEE PHM 2012 Data Challenge (Nectoux et al., 2012), is used to validate the proposed RUL prediction method. This dataset comprises run-to-failure tests on bearings under controlled conditions, simulating real-world operational environments. Vibration signals were collected at a sampling frequency of 25.6 kHz in intervals of 0.1 seconds, recorded every 10 seconds. The dataset includes both horizontal and vertical vibration signals, though only horizontal signals were used in this study due to their higher relevance for bearing degradation (Pichler, Ooijevaar, Hesch, Kastl, & Hammer, 2020).

The dataset consists of 17 bearings tested under three different operating conditions, characterized by varying loads and rotational speeds. For instance, bearings under Condition 1 experienced a load of 4000 N and a speed of 1800 rpm. Table 1 provides a summary of the experimental setup.

Table 1. Summary of the PRONOSTIA dataset.

| Condition | Load (N) | Speed (rpm) | Bearings   |
|-----------|----------|-------------|--|
| 1         | 4000     | 1800        | Learning: 1-1, 1-2, 2-1, 2-2, 3-1, 3-2<br>Testing: 1-3, 1-4, 1-5, 1-6, 1-7 |
| 2         | 4200     | 1650        | Learning: 2-1, 2-2<br>Testing: 2-3, 2-4, 2-5, 2-6, 2-7                     |
| 3         | 5000     | 1500        | Learning: 3-1, 3-2<br>Testing: 3-3   |

To assess the effectiveness of our proposed method for RUL prediction, we evaluated its performance using testing bearings and compared the results with other studies. The evaluation metrics included the score metric, accuracy, and percent error. These metrics are those used in the IEEE PHM 2012 Prognostic Challenge.

The percent error for the  $i$ -th bearing is calculated as follows:

$$Er_i = 100 \times \frac{\text{ActRUL}_i - \hat{\text{RUL}}_i}{\text{ActRUL}_i} \quad (29)$$

where  $\text{ActRUL}_i$  represents the actual RUL, and  $\hat{\text{RUL}}_i$  denotes the predicted RUL of the  $i$ -th testing bearing.

A distinct scoring function to handle overestimations and underestimations differently is used. The scoring function is defined as:

$$Acc_i = \begin{cases} \exp(-\ln(0.5) \times \frac{Er_i}{5}) & \text{if } Er_i \leq 0 \\ \exp(+\ln(0.5) \times \frac{Er_i}{20}) & \text{if } Er_i > 0 \end{cases} \quad (30)$$

In this function, a perfect prediction (i.e., zero percent error) yields a score of 1. As the percent error increases, the score decreases. Notably, predictions that are later than the actual failure time (i.e.,  $Er_i \leq 0$ ) result in a more significant penalty

compared to early predictions.

The overall performance of the RUL prediction is represented by the average score across all testing bearings, calculated as:

$$\text{Score} = \frac{1}{11} \sum_{i=1}^{11} Acc_i \quad (31)$$

#### 3.1.2. Analysis and results

##### (i) Data preparation and processing

Each sample from the PRONOSTIA dataset, consisting of 2,560 data points, undergoes a transformative process to prepare it for input into the ARAL-HI model. Initially, the data is normalized and converted into a  $2560 \times 128$  time-frequency image using the SSWT, capturing intricate signal details. To reduce computational complexity, these high-dimensional images are then compressed into  $128 \times 128$  images through RP, preserving essential features. These processed images are subsequently fed into the ARAL-HI model, which performs regression based on the exponential labeling strategy to accurately assess the degradation of the bearings. Bearing1\_3 is taken as an example in Figure 8 to show the transformations of the time signal through his full life cycle.

##### (ii) Configuration of the ARAL-HI model

The proposed HI model in this study was implemented using Python 3.11 and TensorFlow 2.0, and trained on a high-performance computation server with 2 Tesla V100s-PCI 32Gb GPUs. Extensive hyperparameter tuning and optimization were performed using grid search to ensure optimal performance. The model was trained over 100 epochs with a batch size of 256, using the Adam optimizer with a learning rate of  $3.8e-4$ , striking a balance between convergence speed and stability, and resulting in high accuracy for health assessment tasks. The details of the configuration are presented in Table 2

Table 2. The ARAL model configuration.

| Layer No. | Type                | Filter Size | Activation | Output Shape  |
|-----------|---------------------|-------------|------------|---------------|
| 1         | InputLayer          | -           | -          | (128, 128, 1) |
| 2         | Conv2D              | (7, 7)      | ReLU       | (64, 64, 32)  |
| 3         | MaxPooling2D        | (3, 3)      | -          | (32, 32, 32)  |
| 4         | ResBlock            | (3, 3)      | ReLU       | (32, 32, 64)  |
| 5         | ResBlock            | (3, 3)      | ReLU       | (32, 32, 64)  |
| 6         | ResBlock            | (3, 3)      | ReLU       | (16, 16, 128) |
| 7         | ResBlock            | (3, 3)      | ReLU       | (16, 16, 128) |
| 8         | ResBlock            | (3, 3)      | ReLU       | (8, 8, 256)   |
| 9         | ResBlock            | (3, 3)      | ReLU       | (8, 8, 256)   |
| 10        | Reshape             | -           | -          | (8, 2048)     |
| 11        | Attention Mechanism | -           | Softmax    | (8, 2048)     |
| 12        | LSTM                | 256 units   | -          | (256)         |
| 13        | Flatten             | -           | -          | 256           |
| 14        | Dense               | -           | ReLU       | 2560          |
| 15        | Dropout             | -           | -          | 2560          |
| 16        | Dense               | -           | ReLU       | 512           |
| 17        | Dropout             | -           | -          | 512           |
| 18        | Dense               | -           | Sigmoid    | 1             |



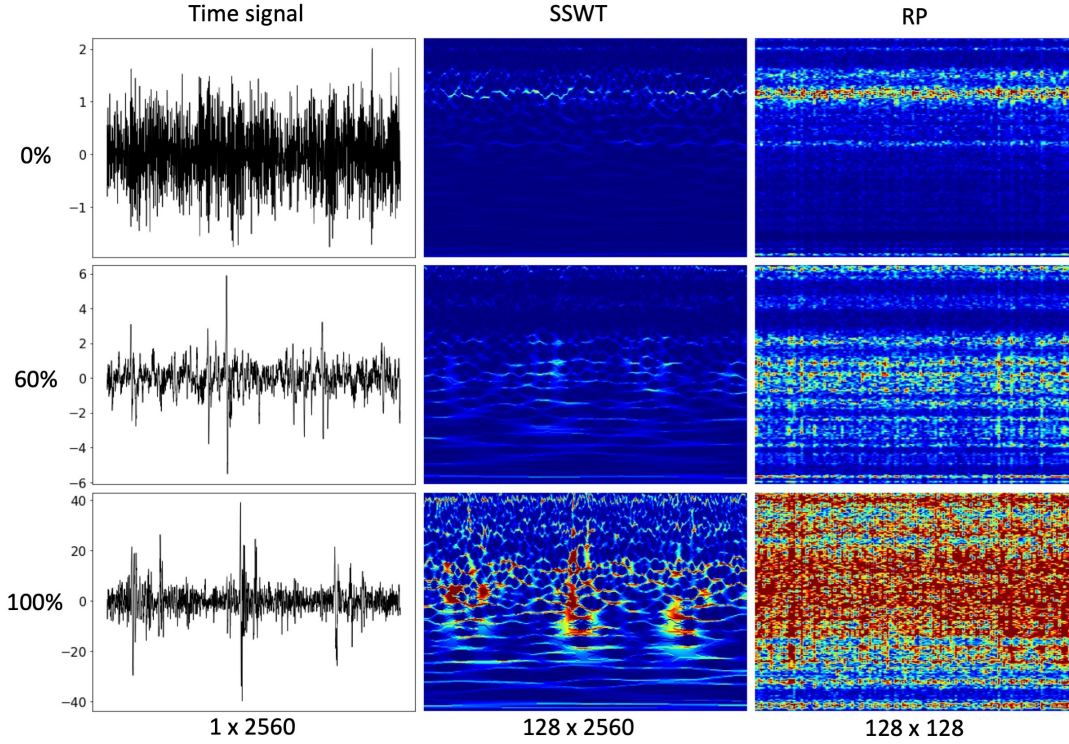


Figure 8. Snapshots of the fault progression of bearing1\_3.

### (iii) The Influence of the Data labeling

Figure 9 illustrates a comparison of RMSE values for the linear and exponential labeling approaches across the three conditions.

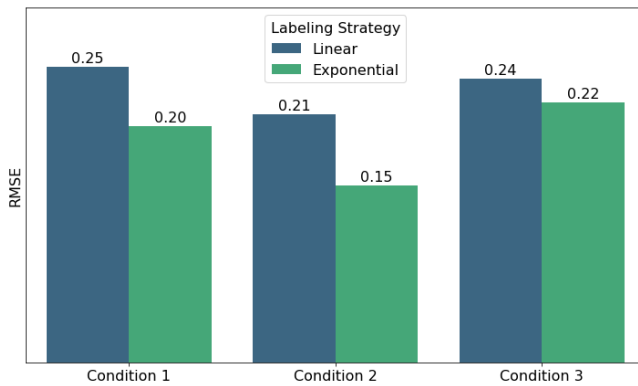


Figure 9. RMSE values for Linear and Exponential Labeling across three conditions.

To assess the impact of different labeling strategies on the prediction performance, we conducted ablation studies focusing on the influence of exponential labeling versus conventional linear labeling of the run-to-failure data. In the conventional linear labeling approach, the HI decreases linearly as the bearing progresses towards failure. Conversely, in the exponential labeling approach, the HI follows an exponential decay pat-

tern, which is designed to provide a more sensitive response to early-stage degradation. We tested these approaches under the three different conditions of the PRONOSTIA dataset. The results indicated that the exponential labeling approach significantly improved the RMSE of the predictions compared to the linear labeling method. Specifically, the exponential model yielded lower RMSE values across all three conditions, facilitating the model's training process and better reflecting the degradation process of the bearing.

### (iv) Number of ResBlocks Selection

We investigated the effect of varying the number of ResBlocks on the model's performance. Specifically, we tested configurations with 2, 4, 6, 8, and 10 ResBlocks. The results, measured in terms of RMSE, indicated that the optimal number of ResBlocks was 6, which yielded the lowest RMSE value. This suggests that having 6 ResBlocks balances model complexity and performance, effectively capturing the necessary features without overfitting.

Figure 10 illustrates the RMSE values for different numbers of ResBlocks.

### (v) Effects of fitting interval selection

When using the full HI data to train and fit our GPR model, it frequently fails to converge due to an abnormal large step phenomenon present in the data. The step-like nature of the

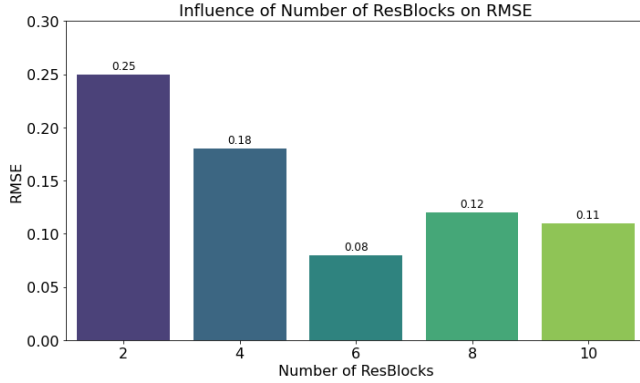


Figure 10. RMSE values for different numbers of ResBlocks.

HI curve leads to significant errors, making accurate RUL estimation challenging and, in many cases, causing the model to never converge to the RUL threshold. However, by incorporating the start fitting point using the 3-sigma method, the model is able to converge and estimate the RUL of the bearing. This improvement is illustrated in Figure 11, which demonstrates the effect using Bearing 1\_4 and 2\_3 as examples.

#### (vi) RUL results

Table 3 presents the RUL prediction results, indicating the error and the accuracy for each bearing. These results are used to benchmark the proposed method against other state-of-the-art techniques. Figure 12 illustrates the RUL prediction process for several test bearings.

Table 3. RUL prediction results of ARAL on PRONOSTIA dataset.

| Bearing Number | Current Time (s) | Actual RUL (s) | Predicted RUL (s) | Error   | Accuracy |
|----------------|------------------|----------------|-------------------|---------|----------|
| 1_3            | 18010            | 5730           | 5610              | 2.0942  | 0.9300   |
| 1_4            | 11380            | 339            | 320               | 5.6047  | 0.8235   |
| 1_5            | 23010            | 1610           | 1290              | 19.8758 | 0.5022   |
| 1_6            | 23010            | 1460           | 1510              | -3.4247 | 0.9336   |
| 1_7            | 15010            | 7570           | 7430              | 1.8494  | 0.9379   |
| 2_3            | 12010            | 7530           | 7880              | -4.6481 | 0.9063   |
| 2_4            | 6110             | 1390           | 1390              | 0.0000  | 1.0000   |
| 2_5            | 20010            | 3090           | 2640              | 14.5631 | 0.6037   |
| 2_6            | 5710             | 1290           | 1290              | 0.0000  | 1.0000   |
| 2_7            | 1710             | 580            | 600               | -3.4483 | 0.9333   |
| 3_3            | 3510             | 820            | 760               | 7.3171  | 0.7760   |

### 3.1.3. Comparison and Analysis of RUL Prediction Methods

This section presents a comparative analysis between the proposed method and seven leading techniques to highlight its effectiveness and superiority. The results of the experiments, illustrated by the box plots in Figure 13 and detailed in Table 4, provide a comprehensive summary of the performance of the eight RUL prediction methods on the PRONOSTIA

dataset.

Among the seven comparative methods:

- (Liu, Song, Yang, Hao, & Peng, 2018) utilized health indicators derived from the Hilbert–Huang transform (HHT) to predict the RUL of bearings;
- (Wang, Lei, Li, & Li, 2020b) introduced an approach combining an exponential degradation model with a relevance vector machine (RVM) to estimate the RUL, referred to as EMD-RVM;
- (She & Jia, 2021) developed a bidirectional gated recurrent unit (Bi-GRU) model, enhanced with bootstrap techniques, for RUL prediction;
- (L. Li et al., 2023) proposed a multi-technique fusion method for health prognostics, integrating relevance vector machine with a deep separable convolutional gated recurrent network (DSGGRN);
- (Zhuang, Jia, Cao, & Zhao, 2022) implemented a semi-supervised approach, utilizing a double attention guided assessment method (SDAGA), for estimating the RUL;
- (Hong, Zhou, Zio, & Hong, 2014) employed wavelet packet-empirical mode decomposition (WP-EMD) for feature extraction, followed by self-organizing mapping (SOM) for assessing performance degradation, named WP-EMD-SOM;
- (Chen, Jin, Kong, Wang, & Xu, 2023) introduced a Global and Local Information Integrated Network (GLIIN) for predicting the remaining useful life of bearings.

Based on the error ( $Er$ ) formula, if  $Er < 0$ , it means the predicted RUL is longer than the actual RUL, which is detrimental to equipment safety. The proposed method has three cases of negative errors, similar to HHT and DSGGRN. In contrast, methods like Bi-GRU and GLIIN exhibit a higher frequency of negative errors, with 4-6 occurrences. This suggests that the proposed method matches the safety assurance levels of the top-performing methods, and maintains a lower rate of unsafe predictions.

The box plot of errors indicates the distribution and spread of the error percentages for each method. The reference line at Error = 0 signifies the ideal scenario where predicted RUL matches the actual RUL perfectly. Methods like HHT, EDM-RVM, Bi-GRU, show a wide spread in error distribution, indicating variability in their predictions. DSGGRN and SDAGA display more compact error distributions, suggesting higher consistency and accuracy. WD-EMD and GLIIN have significant error spreads, demonstrating occasional large deviations from the actual RUL. The proposed method exhibits a relatively narrow error distribution, with most errors close to zero, indicating high accuracy and consistency.

The box plot of accuracies indicates the distribution and spread of the accuracy scores for each method. The reference

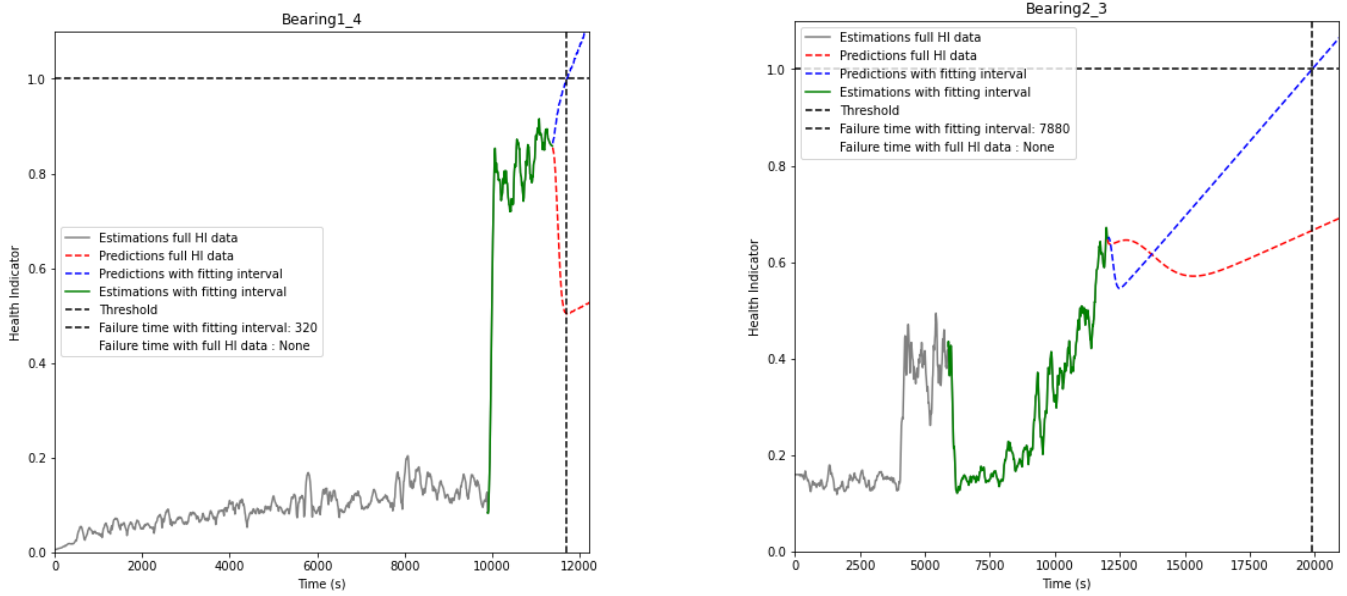


Figure 11. Effect of fitting interval selection

Table 4. State-of-art methods' results comparison with the proposed method.

| Dataset      | HHT<br>(Er%) | EDM-RVM<br>(Er%) | Bi-GRU<br>(Er%) | DSGGRN<br>(Er%) | SDAGA<br>(Er%) | WP-EMD-SOM<br>(Er%) | GLIIN<br>(Er%) | Proposed<br>(Er%) |
|--------------|--------------|------------------|-----------------|-----------------|----------------|---------------------|----------------|-------------------|
| Bearing 1_3  | 2.58         | -1.05            | -4.36           | 6.32            | 3.66           | -1.04               | 0.87           | 2.09              |
| Bearing 1_4  | -9.14        | -17.99           | 70.50           | -7.67           | 2.65           | -20.94              | -131.91        | 5.60              |
| Bearing 1_5  | -0.99        | 21.74            | 6.21            | 14.90           | -4.35          | -278.26             | -109.29        | 19.88             |
| Bearing 1_6  | 6.03         | 6.16             | -4.11           | 13.42           | -0.68          | 19.18               | 5.27           | -3.42             |
| Bearing 1_7  | -0.70        | 7.79             | 18.63           | -0.96           | 10.57          | -7.13               | -10.31         | 1.85              |
| Bearing 2_3  | 55.44        | 43.03            | 17.40           | 19.31           | 0.93           | 10.49               | 47.97          | -4.65             |
| Bearing 2_4  | 15.56        | 1.44             | -1.44           | 4.53            | -5.76          | 51.80               | 4.24           | 0.00              |
| Bearing 2_5  | 49.19        | 18.77            | 5.18            | -2.69           | -2.27          | 28.80               | 0.88           | 14.56             |
| Bearing 2_6  | 38.53        | 2.33             | 16.25           | 3.02            | -5.43          | -20.93              | 2.34           | 0.00              |
| Bearing 2_7  | 5.17         | -3.45            | 10.34           | 2.24            | 56.90          | 44.83               | -138.40        | -3.45             |
| Bearing 3_3  | 2.56         | 13.41            | 6.10            | -14.15          | 2.44           | -3.66               | 0.98           | 7.32              |
| <b>Score</b> | 0.6101       | 0.5941           | 0.6190          | 0.6832          | 0.6928         | 0.3550              | 0.5413         | 0.7582            |

line at Accuracy = 0.6 marks the threshold for good prediction performance. HHT, EDM-RVM, and Bi-GRU show wide distributions around this threshold. For instance, the interquartile range (IQR) for HHT spans from approximately 0.4 to 0.75, suggesting variability in performance. The median accuracy for these methods is near or above 0.6, but the spread indicates that their predictions are not consistently reliable. DSGGRN and SDAGA have more compact distributions, with the majority of their accuracy scores above 0.6. The IQR for DSGGRN is approximately 0.55 to 0.85, and for SDAGA, it is about 0.65 to 0.85. These narrow IQRs reflect higher consistency and reliability in their predictions. WD-EMD and GLIIN exhibit significant variability, with fewer accuracy scores consistently exceeding 0.6. The IQR for WD-

EMD is wide, from approximately 0.3 to 0.75, indicating less reliable performance. Similarly, GLIIN has a broad IQR ranging from about 0.4 to 0.7, suggesting variability and occasional poor predictions. The proposed method demonstrates a consistently high performance, with a compact distribution well above the 0.6 threshold. The IQR for the proposed method spans from approximately 0.75 to 0.85, and the median accuracy is around 0.8. This indicates superior stability and effectiveness. Over 75% of the cases achieve a score above 0.6, underscoring the method's robustness and reliability.

Among the eight methods, the proposed method has the lowest number of cases where the predicted RUL is larger than

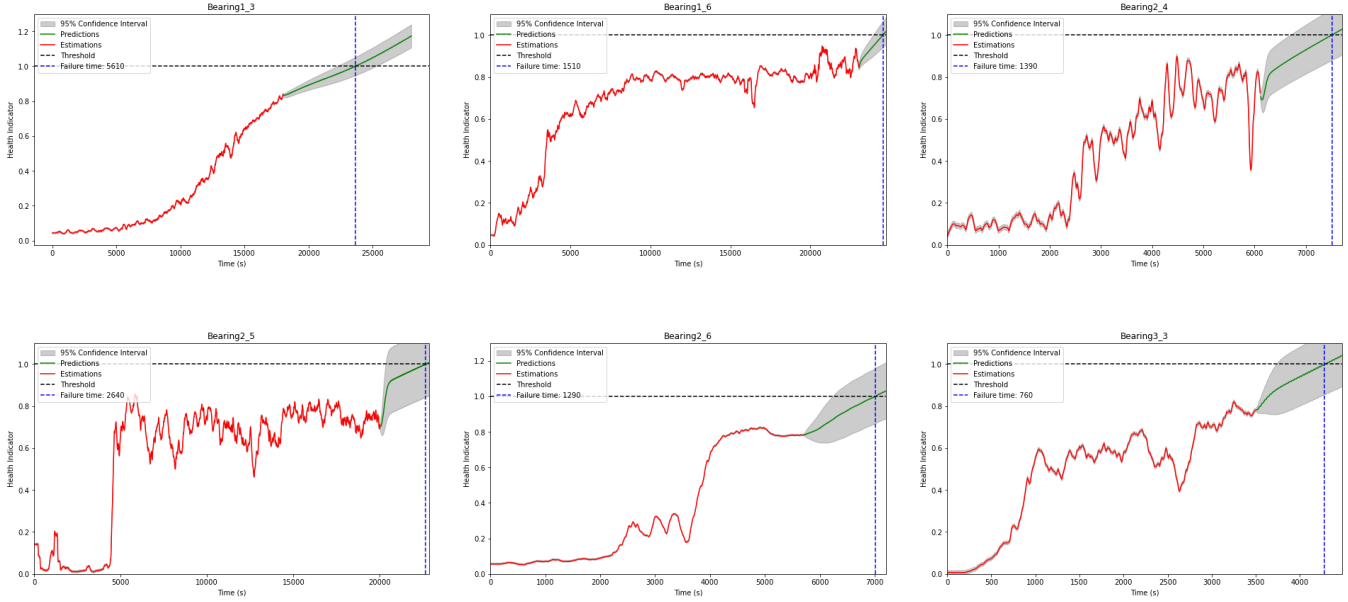


Figure 12. RUL prediction for some bearings

the actual RUL, which is crucial for ensuring equipment safety. The score of the proposed method is 0.7582, higher than the other methods. This improvement in score highlights the superior overall prediction performance of the proposed method. The box plots further illustrate the proposed method's stability and accuracy, with the least variability in errors and the highest consistency in achieving good accuracy scores. The proposed method demonstrates the best balance between low prediction errors and high accuracy, making it the most reliable method among those compared.

However, despite its strong overall performance, it is important to acknowledge certain limitations. A more detailed analysis reveals that for bearings with RULs under 1000 seconds (such as bearings 1\_4, 2\_7, and 3\_3), the SDAGA method outperforms the proposed method in 2 out of the 3 instances. This indicates that in cases of shorter RUL predictions, our method may exhibit slight underperformance compared to SDAGA. While our method provides higher overall accuracy and stability, these observations suggest that further refinement might be needed to handle fast-degrading components more effectively.

This insight is critical for future users to understand the specific contexts in which the proposed method is most effective and where alternative methods may be more appropriate. Despite this limitation, the proposed method remains highly effective for general use, offering the best balance between low prediction errors and high accuracy across a wide range of bearings, as shown by the overall results.

## 3.2. Case study 2: XJTU-SY datasets

### 3.2.1. Experimental setup and evaluation metrics

The XJTU-SY rolling bearing dataset, developed by (Wang et al., 2020a), provides comprehensive vibration data for 15 rolling element bearings (model LDK UER204) under accelerated degradation conditions. The testbed consists of an AC induction motor, speed controller, support shaft, hydraulic loading system, and two heavy-duty roller bearings. Vibration signals are collected using two PCB352C33 accelerometers in both vertical and horizontal directions with a sampling frequency of 25.6 kHz, a sampling interval of 1 minute, and a duration of 1.28 seconds per sample. The dataset captures the full life cycle of the bearings across three operating conditions, with five bearings tested under each condition. These conditions involve varying radial forces and rotational speeds, simulating different stress levels on the bearings, as detailed in Table 5. The dataset documents two primary degradation trends—slow and abrupt—providing valuable data for training and testing predictive maintenance models.

For the assessment of predictive performance on this dataset, we use two key metrics: RMSE and Score (Saxena, Goebel, Simon, & Eklund, 2008), defined as:

$$\text{RMSE} = \sqrt{\frac{1}{Q} \sum_{i=1}^Q d_i^2} \quad (32)$$

where  $Q$  is the number of testing samples, and  $d_i = \text{PreRUL}_i - \text{ActRUL}_i$  represents the error between the predicted RUL and the actual RUL for the  $i$ -th sample.

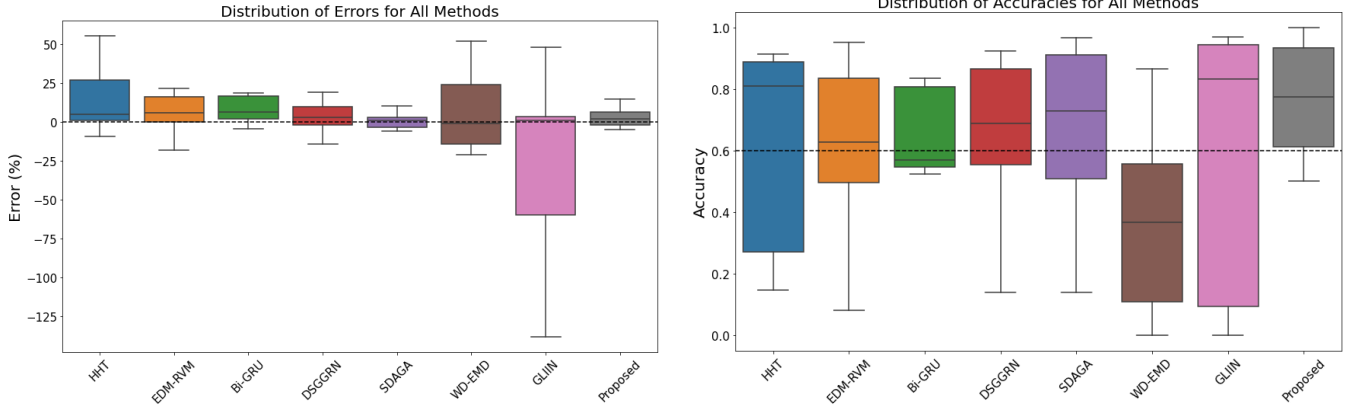


Figure 13. Distribution of RUL prediction errors and accuracies for the compared methods.

$$\text{Score} = \sum_{i=1}^Q \begin{cases} \exp\left(-\frac{d_i}{13}\right) - 1 & \text{if } d_i < 0 \\ \exp\left(\frac{d_i}{10}\right) - 1 & \text{if } d_i \geq 0 \end{cases} \quad (33)$$

where  $d_i$  is as defined above.

Table 5. Operating conditions and corresponding bearing datasets of XJTU-SY.

| Condition | Radial Force (kN) | Shaft Speed (rpm) | Bearings                                       |
|-----------|-------------------|-------------------|--|
| 1         | 12                | 2100              | Learning: 1.1, 1.2<br>1.3, 1.4<br>Testing: 1.5 |
| 2         | 11                | 2250              | Learning: 2.1, 2.2<br>2.3, 2.4<br>Testing: 2.5 |
| 3         | 10                | 2400              | Learning: 3.1, 3.2<br>3.3, 3.4<br>Testing: 3.5 |

### 3.2.2. Analysis and results

#### (i) Data preparation and processing

For the XJTU-SY dataset, each file contains 32400 data points, from which 2560 data points are randomly selected for simplicity. The selected data is then processed similarly to the PRONOSTIA dataset, undergoing normalization, transformation into  $2560 \times 128$  TF images via SSWT, and dimensionality reduction to  $128 \times 128$  images through RP. These images are subsequently fed into the ARAL-HI model for regression using the exponential labeling strategy to assess bearing degradation. The same model configuration for ARAL, presented in Table 2, is used in this experiment for model training and HI construction.

#### (ii) Experiment results

To ensure the robustness of our RUL predictions and reduce the impact of randomness, each experiment was repeated 20

times for the test bearings. We specifically focused on calculating the score and RMSE from the midpoint to the end of each bearing's lifetime, as predictions during this period are more reliable and meaningful due to the clearer degradation patterns (Singleton, Strangas, & Aviyente, 2015). By averaging the results over these 10 repetitions, we were able to obtain stable and accurate assessments of the model's performance, reflecting its true predictive capability during the critical later stages of bearing life. The RUL prediction results are presented in Table 6.

#### 3.2.3. Comparison and Analysis of RUL Prediction Methods

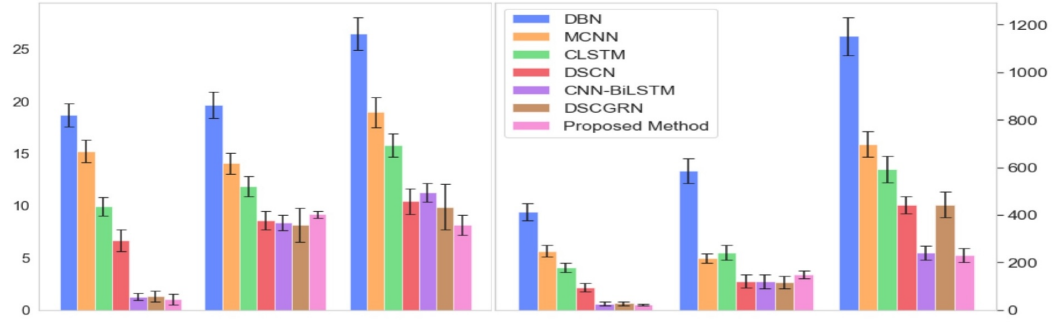
The Figure 14 provides a comparative analysis of various methods for predicting the RUL of bearings 1.5, 2.5, and 3.5, using both RMSE and SCORE metrics. Both metrics assess prediction accuracy, but with different emphases: RMSE maintains consistency across early and late predictions, while SCORE imposes tougher penalties on late predictions, as shown in the histograms. The methods compared include DBN (Deutsch & He, 2018), MCNN (Zhu, Chen, & Peng, 2019b), CLSTM (Zhao, Yan, Wang, & Mao, 2017), DSCN (Wang, Lei, Li, & Yan, 2019), CNN-BiLSTM (Cheng, Hu, Wu, Zhu, & Shao, 2021), DSCGRN (L. Li et al., 2023), and the Proposed Method.

For Bearing 1.5, the Proposed Method exhibits the lowest RMSE ( $1.02 \pm 0.50$ ) and SCORE ( $22.23 \pm 3.10$ ), indicating superior prediction accuracy. In contrast, for Bearing 2.5, DSCGRN outperforms the Proposed Method, achieving a lower RMSE ( $8.13 \pm 1.64$ ) and SCORE ( $116.29 \pm 25.45$ ). This suggests that DSCGRN is better at managing late prediction errors, which are more heavily penalized by the SCORE metric.

The results for Bearing 3.5 further emphasize the strength of the Proposed Method, which again achieves the lowest

Table 6. RUL prediction results for bearings 1\_5, 2\_5, and 3\_5.

| Bearing Number | Full Lifetime (min) | Starting Time (min) | RMSE (mean $\pm$ std) | Score (mean $\pm$ std) |
|----------------|---------------------|---------------------|-----------------------|------------------------|
| 1_5            | 52                  | 26                  | $1.02 \pm 0.50$       | $22.23 \pm 3.10$       |
| 2_5            | 339                 | 170                 | $9.15 \pm 0.34$       | $149.02 \pm 15.50$     |
| 3_5            | 114                 | 57                  | $8.14 \pm 0.96$       | $230.97 \pm 30.20$     |



| Method          | RMSE (mean $\pm$ std) |                  |                  | Score (mean $\pm$ std) |                    |                     |
|-----------------|-----------------------|------------------|------------------|------------------------|--------------------|---------------------|
|                 | Bearing 1.5           | Bearing 2.5      | Bearing 3.5      | Bearing 1.5            | Bearing 2.5        | Bearing 3.5         |
| DBN             | $18.68 \pm 1.13$      | $19.62 \pm 1.28$ | $26.48 \pm 1.56$ | $413.97 \pm 36.26$     | $585.02 \pm 51.27$ | $1151.95 \pm 79.70$ |
| MCNN            | $15.22 \pm 1.07$      | $14.04 \pm 0.97$ | $18.93 \pm 1.43$ | $247.76 \pm 23.81$     | $217.38 \pm 20.83$ | $696.99 \pm 53.25$  |
| CLSTM           | $9.89 \pm 0.89$       | $11.84 \pm 0.94$ | $15.78 \pm 1.12$ | $178.94 \pm 20.37$     | $241.06 \pm 31.52$ | $592.15 \pm 54.56$  |
| DSCN            | $6.67 \pm 1.04$       | $8.58 \pm 0.92$  | $10.41 \pm 1.21$ | $94.91 \pm 17.05$      | $121.03 \pm 26.54$ | $441.20 \pm 36.10$  |
| CNN-BiLSTM      | $1.27 \pm 0.32$       | $8.37 \pm 0.76$  | $11.27 \pm 0.88$ | $26.75 \pm 7.25$       | $119.74 \pm 28.69$ | $241.06 \pm 30.16$  |
| DSCGRN          | $1.33 \pm 0.52$       | $8.13 \pm 1.64$  | $9.87 \pm 2.20$  | $28.26 \pm 8.14$       | $116.29 \pm 25.45$ | $443.83 \pm 55.23$  |
| Proposed Method | $1.02 \pm 0.50$       | $9.15 \pm 0.34$  | $8.14 \pm 0.96$  | $22.23 \pm 3.10$       | $149.02 \pm 15.50$ | $230.97 \pm 30.20$  |

Figure 14. Performance comparison of different prognosis methods on the XJTU-SY dataset.

RMSE ( $8.14 \pm 0.96$ ) and SCORE ( $230.97 \pm 30.20$ ). Overall, the Proposed Method demonstrates robust performance across different bearings, excelling particularly in minimizing prediction errors. However, the slightly better performance of DSCGRN in Bearing 2.5 highlights that certain methods may be more effective under specific conditions, particularly in avoiding late RUL predictions.

#### 4. CONCLUSION & FUTURE WORK

This paper introduced ARAL, an advanced method for predicting the RUL of rolling bearings by integrating SSWT, RP, ResNet, a Temporal Attention Mechanism, and LSTM models. The method effectively captures critical time-frequency features, addressing challenges like the vanishing gradient problem and enhancing prediction accuracy. Experimental results on the PRONOSTIA and XJTU-SY datasets demonstrate that ARAL outperforms existing techniques in terms of accuracy and reliability, achieving lower RMSE and higher prediction scores across various test cases. The use of exponential data labeling and GPR further improves RUL predictions, particularly in accurately capturing degradation trends and reducing prediction errors, making ARAL a robust tool for industrial prognostics and health management.

While ARAL shows strong overall performance, there are some limitations related to its real-time application. The primary challenge lies in the execution time required during the GPR fitting phase, particularly when processing long HI curves. This step can significantly slow down the prediction process, which could impact ARAL's usability in time-sensitive industrial environments. Optimizing the GPR process through model simplification or faster approximation techniques will be a key focus for future work to ensure that ARAL meets real-time performance requirements without compromising accuracy.

Additionally, ARAL demonstrates slight underperformance in predicting rapidly degrading components, such as bearings with shorter RULs. Addressing this limitation through further model refinements will also be explored. Future work will involve extending ARAL to other machinery types, integrating additional data sources, and improving the method's robustness and computational efficiency for broader industrial applicability.

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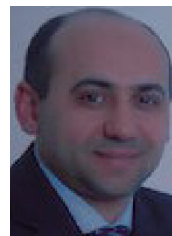
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